Rapid Rekeying Using Markov Models

by Paul L. Yu, Brian M. Sadler, and John S. Baras
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Rapid Rekeying Using Markov Models

Paul L. Yu and Brian M. Sadler
Computational and Information Sciences Directorate, ARL

John S. Baras
University of Maryland
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Keys replacement is a central problem in key management. We introduce a novel rekeying method that uses Markov models to efficiently provide fresh keys with perfect forward secrecy and resistance to known-key attacks, while removing the need for extra communications or third parties. These constraints are motivated by wireless devices, where communications are expensive and infrastructure is not guaranteed. The efficiency of the method allows keys to be replaced much more often and enhances session security.
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1. Introduction

In this report we consider how two parties can rapidly and securely replace their shared symmetric encryption keys. Our randomized algorithm produces nondeterministic key sequences whose recovery is difficult for adversaries and yet easy for intended parties. We label the keys used for data encryption as *temporal*. We assume that the parties also share a *session key* that is used to rekey the temporal keys. Rekeying is necessary because keys can be compromised by adversaries; the possibility of a key compromise increases with the frequency of its use \((1, 2)\). It is therefore important to replace the temporal key before compromise is probable, and much sooner than that, if possible. Our distinction between key types indicates that the temporal keys, since they are constantly being used for encryption, should be replaced much more often than the session key. However, unless efficient rekeying algorithms are used, the additional protection of the temporal keys may require significant overhead. This is of particular concern in energy constrained devices such as in mobile ad-hoc or sensor networks.

Symmetric keys are often used for high rate transfers because encryption/decryption has relatively low complexity. Further, it is well known that in terms of security per bit, symmetric keys are the strongest \((3)\) (followed by elliptic curve \([4, 5]\) and asymmetric keys \([6]\)). That is, for the same length key, symmetric key systems are the hardest to defeat. However, the main obstacle of using symmetric encryption is the difficulty in distributing and replacing the keys. The three main philosophies used to generate, and occasionally replace, the initial session keys are not suited for the rapid rekeying of the temporal keys for various reasons:

1. Distributing secret keys over a secure channel (e.g., \([7]\)) is not always a suitable solution because it assumes the availability of a separate secure channel. For example, this is hard to achieve in wireless situations. There is a fundamental tradeoff between how many keys are initially distributed and how long before the secure channel is needed again to rekey.

2. Negotiating keys over an insecure channel (e.g., \([8, 9]\)) can be expensive in terms of communication and computation. Handshaking messages are generally required to establish the new key. As the rate of rekeying increases, the computation and communication costs become prohibitive.

3. Relying on third parties to help manage keys (e.g., \([10]\)) is not always an option (in mobile ad-hoc networks, for example \([11]\)). Even if the computational load is pushed to the third party, the fundamental cost of using the channel to distribute keys is that rekeying messages take the place of data and hence reduce the data rate.
When a symmetric key is used to encrypt traffic, the adversary has more information that allows her to possibly recover the key. Therefore, the keys are typically reestablished through another round of authentication and key negotiation (as in the previous references), where both parties contribute entropy towards the next shared key. However, if the rekeying can occur often enough, there is very little possibility of compromise by the adversary, and the precautions of reauthentication and renegotiation may not be strictly necessary. In our proposed method, we have a session key that helps generate the temporal keys that are used for encryption. By changing the temporal keys rapidly, it is difficult for an adversary to compromise them. Further, by selecting temporal keys in a nondeterministic way, it is very difficult for an adversary to gain information about the session key.

We are motivated by the unsuitability of standard keying methods for use over constrained devices and use the preceding reasoning to arrive at a novel method that exploits the randomness of Markov models to efficiently replace the temporal keys. In this report we show that the proposed key replacement method:

- produces sequences of temporal keys with a positive key entropy rate
- does not require explicit key replacement communication between the sender and receiver
- does not require the presence or cooperation of trusted third parties
- has very low storage requirements
- has computational requirements comparable to or lower than other secure key replacement methods
- increases the difficulty for the adversary to gain session key information

We quantify the security of our key replacement method by the equivocation of the generated keys. With careful selection of parameters, we show that key security can be very high with only modest communication, computation, and memory requirements. In particular, we show that it is difficult for adversaries to deduce the current temporal key. Further, even when able to compromise the temporal key, the adversary is unable to gain significant advantage in deducing past or future keys because the session key remains well protected.
2. Problem Overview

Any rekeying method must satisfy some security requirements in order to be useful. A method that is also efficient allows for more frequent key replacements; this can enhance system security. We detail first our security requirements and then our efficiency metrics.

2.1 Key Security

We assume the following scenario. Alice and Bob share a pre-distributed session key $l$, which is used to select a Markov model from a large collection. This model is used to generate all the temporal keys $\{k_i\}$ that will be used. They use the temporal key $k_i$ to encrypt their messages in the $i^{th}$ epoch. In the next epoch, they replace it with the fresh key $k_{i+1}$.

There is an adversary, Eve, who wants to deduce the secret keys (session or temporal) given her observations of the encrypted messages. We are interested in the ability of Eve to deduce the secret keys both as an outsider* and as a one-time insider.† In particular, when Eve is a one-time insider we are concerned about the secrecy of past keys (perfect forward secrecy) and future keys (susceptibility to known-key attacks) (12).

Perfect forward secrecy refers to the protection of past temporal keys given the compromise of the session key. That is, if Eve obtains the session key $l$ during epoch $i$, she is unable to infer the temporal keys used in prior epochs $\{k_1, \ldots, k_{i-1}\}$ above a small probability (the messages remain secret forward in time). The resistance of the method to known-key attacks refers to the protection of future temporal keys given knowledge of past temporal keys (but not the session key). Taken together, these two requirements state that in the event of a key breach, Eve is able to recover past or future temporal keys with only a small probability.

2.2 Replacement Efficiency

The efficiency of a key replacement algorithm or method can be quantified in a variety of ways:

---

*An outsider knows only what is generally available (e.g., the key replacement method) but not privileged information (e.g., any of the keys).
†An insider (cf. outsider) has access to privileged information (e.g., one or more keys); a one-time insider gains such information at only one point in time.
• Number and bandwidth of messages required
• Complexity of the computation at Alice and Bob, measured by the number of simple operations
• Size of storage and memory requirements

In this report, we demonstrate a method that can generate high quality key replacements without requiring explicit key replacement communications or unreasonable amounts of memory. We accomplish this by using large Markov models in a synchronized way to choose the replacement keys. However, the transitions between states are random; this has the effect of exponentially increasing Eve’s search space while our method keeps the search space of Alice and Bob manageable.

The storage requirements are minimized by using a pseudo-random number generator (PRNG) to generate only the portions of the Markov model in use. This avoids the need for Alice and Bob to store the entire model in memory. As we discuss in section 4, reliance upon a PRNG is a potential vulnerability and thus we require PRNGs that are cryptographically secure. Secure PRNGs generally require more computations than non-secure PRNGs, and a variety of them exist, offering varying levels of security and complexity. We note that the computational requirement of our method is comparable with other secure key replacement methods. In section 7 we contrast our new approach with some existing key exchange methods, exploring the various tradeoffs between security and efficiency.

3. Markov Key Replacement Method

We introduce our key replacement method with a simple example. We assume that Alice and Bob synchronize their key replacements, e.g., they may agree to change their keys at regular time intervals.

Illustrating Example:

Suppose that there is a large family of Markov models. Let Alice and Bob choose the particular model shown in figure 1. Eve does not know which model is chosen. Each model state represents a unique temporal key. Suppose that Alice and Bob are currently using
Figure 1. Simple Markov model when $K = 4$ and $b = 2$. The states and possible transitions are shown in (a) while a corresponding probability matrix is shown in (b). Note that $A$ is sparse.

key 2. At the next key replacement time, Alice starts to use either key 1 or key 3 with equal probability. Suppose Alice chooses key 1.

Bob, having both the model and the current key, knows that the replacement key is either 1 or 3. He is able to determine which key is correct by checking the message integrity (detailed below) after decrypting with each possible key. After the check, Bob knows that Alice is using key 1, and starts to use key 1. Alice and Bob thus regain synchrony. These steps are repeated at each key replacement time.

Note that for each rekey, Alice makes a random (constrained) decision on the next temporal key. This adds entropy to the rekeying step and is the fundamental difference between this method and the use of a seeded PRNG’s output as the sequence of temporal keys. That method has the illusion of increasing key randomness but the sequence is actually deterministic given the initial seed; in comparison, by making the random key choice Alice increases the entropy of the key sequence with each rekey (section 4.4).

In the following sections, we describe how the temporal keys are used to encrypt messages and how Bob determines if he is using the correct key. This ability to identify the correct key is a central assumption in the proposed method. Then, the specification and construction of the family of Markov models are detailed, and their use is described in the context of Alice and Bob’s key replacement algorithms. Finally, we analyze the efficiency of the method.
3.1 Message Model

We use the superscripts $a, b$ to denote the influence or ownership of Alice or Bob, respectively.

During key epoch $i$, Alice forms the ciphertext $x_i$ by encrypting the message $s_i^a$ with her temporal key $k_i^a$

$$x_i = f_e(s_i^a, k_i^a), \quad (1)$$

and Bob recovers the message by decrypting the ciphertext with his key

$$s_i^b = f_d(x_i, k_i^b). \quad (2)$$

The encryption and decryption functions satisfy

$$s = f_d(f_e(s, k), k) \quad (3)$$

and hence when $k_i^a = k_i^b$ Bob receives the message correctly ($s_i^b = s_i^a$).

We assume that the message includes an integrity check so that the receiver knows when the message is received correctly. For example, the message may be appended with a cyclic redundancy check (CRC)-32 which will match when the correct key is used to decrypt. Writing the integrity check as $\psi(\cdot)$, we test a particular key $m$ with the message $x_i$:

$$\psi(x_i, m) = \begin{cases} 0 & \Rightarrow s_i^a \neq s_i^b \text{ or } k_i^a \neq m \\ 1 & \Rightarrow s_i^a = s_i^b \text{ and } k_i^a = m \end{cases}. \quad (4)$$

That is, when the integrity check fails ($\psi(\cdot) = 0$), Bob is certain that the message is received in error or that the tested key is incorrect (mismatched with Alice’s key). Conversely, when the integrity check passes, Bob knows that the message and key are both correct. Therefore, Bob can use the outcome of $\psi(\cdot)$ to determine if he is using the correct key.

For clarity of the following discussion, we assume that a passed integrity check implies perfect message reception with the correct key. However, in actuality, there may be a non-zero probability that an incorrect key or message can lead to a passed integrity check. For instance, it is possible to pass a CRC check when the incorrect key was used to decrypt. We elaborate on the effect of such errors in section 6.

3.2 Family of Markov Models

Alice and Bob choose the same Markov model $\lambda$ from a large family of models $\Lambda$ using an index $l$. We view $l$ as the session key shared by Alice and Bob. For security, let each model
be chosen with equal probability $1/L$, where $|\Lambda| = L$. They use this model to determine the subsequent temporal keys that they will use to encrypt/decrypt their traffic. There should be many possible Markov models and temporal keys to resist successful brute-force attacks.

### 3.2.1 Markov Model Specification

Denote a Markov model by $\lambda = (A, \pi)$, where $A$ is the transition probability matrix and $\pi$ contains the initial key probabilities. Suppose that the temporal keys are drawn from a keyspace $\mathcal{K}$ with size $K$, i.e., $|\mathcal{K}| = K$. Then $A$ is a $K \times K$ matrix and $\pi$ is a $K \times 1$ column vector. We use the convention that $A(m, n)$ is the probability of transitioning from key $m$ to key $n$, and likewise $\pi(m)$ is the probability of having initial key $m$.

Looking forward to section 3.3, we limit the complexity of the receiver by allowing each key to transition to one of exactly $d$ possible keys. We call $d$ the branching factor of the model and specify that the key transitions are equiprobable. That is, if a transition from key $m$ to $n$ exists, it is taken with probability $1/d$.

$$\sum_n I(A(m, n)) = d, \forall m \tag{5}$$

$$A(m, n) \in \{0, \frac{1}{d}\}, \forall m, n \tag{6}$$

When $d \ll K$, the transition matrix is sparse.

### 3.2.2 Construction

We motivate our Markov model construction method by first considering the memory requirements of a naive approach. A single Markov model requires $O(dK)$ memory, since limiting the branching factor $d$ makes the number of total transitions linear in $K$. For 32-bit keys with branching factor 2, the model requires at least 1 gigabyte of memory.

Storing the entire family of $L$ Markov models thus requires $O(dKL)$, and quickly becomes infeasible when $L$ or $K$ grow large. Even with small key sizes $L = K = 2^{32}$ and a modest branching factor of $d = 2$, the storage requirement is approximately $2^{32+32+1}$, or 4.3 billion gigabytes. Clearly, storing entire models in memory is not feasible when realistic key sizes are considered.

Note that Alice and Bob only need to know the current key and the set of possible next keys in order to replace their temporal key. We therefore turn our attention towards an algorithm that allows Alice and Bob to directly access the transition probabilities from any given key without having to store the entire model in memory. Note that specifying the possible transitions from each state is equivalent to specifying the Markov model.
Let us assume $q$-bit temporal keys. Given the current key $k_i = m$, how do we find the set of possible next keys, i.e., the set of $n$ for which $A(m, n)$ is nonzero? One possibility is diagrammed in figure 2 and outlined below:

1. Seed a PRNG with a value $f(l, m)$, where $l$ is the session key and $m$ is the value of the current temporal key $k_i$. For the experiments in this report we use

$$f(l, m) = K*l + m$$ (7)

though, in general, $f(\cdot)$ can be any deterministic mapping.

2. Select $q$-bit segments of the PRNG output. Each segment corresponds to a candidate for the next key. Repeat until there are $d$ unique keys.

3. The transition probabilities of each candidate key are $1/d$.

![Figure 2. Construction and use of a random access Markov model with 4-bit temporal keys. PRNG is seeded based on the current key and model to generate the set of next keys.](image)

Note that we reseed the PRNG each time we calculate transition probabilities from a different key. For the remainder of this report we assume that the Markov models appear statistically random. This is true for a good PRNG, the requirements of which are described in section 4.

Let $\pi(1) = 1$ so that the initial temporal key is $k_0 = 1$. This key is not used to encrypt any messages because it is known to everyone, but it is used to generate the first temporal key $k_1$. We elaborate on this in the next section.

### 3.3 Key Replacement Algorithm

Before we present the simple key replacement algorithms, we first define the goal of key replacement methods in terms of key synchrony.
**Definition 1** The keys of Alice and Bob are synchronized for \( n \) key epochs when

\[
    k_i^a = k_i^b, \forall 0 \leq i < n
\]  

(8)

**Definition 2** The time-to-failure of the method is \( n_0 \), where

\[
    n_0 = \arg \min_{i>0} k_i^a \neq k_i^b
\]  

(9)

We wish to assert that \( n_0 \), the time-to-failure, is large. We show that \( n_0 = \infty \) when the integrity check is perfect (section 3.3). The synchrony time for imperfect integrity checks is addressed in section 6.

We now introduce the key replacement algorithm. We assume that messages are transmitted starting in epoch 1 so that the first temporal keys are \( k_1^a \) and \( k_1^b \).

**Initialization:**

1. Alice and Bob choose a Markov model

\[
    \lambda^a = \lambda^b = \Lambda(l),
\]  

where integer \( l \) is chosen uniformly from \( \{1, \ldots, |\Lambda|\} \)

2. Alice and Bob initialize their temporal keys

\[
    k_0^a = k_0^b = 1.
\]  

(11)

3. Alice performs a **Key Replacement** (below) to select the first temporal key \( k_1 \).

**Key Replacement:**

Alice uses \( l \) and \( k_i^a \) to generate the next temporal key \( k_{i+1}^a \), which is used to encrypt the messages in epoch \( i + 1 \). She does not explicitly signal any key information to Bob.

1. Find the set of possible keys from \( k_i^a \): \( \mathcal{N} = \{n|A(k_i^b, n) > 0\} \). See figure 2 or section 3.2.2 for details.

2. Assign \( k_{i+1}^a = n \in \mathcal{N} \) w.p. 1/d
Key Recovery:

At the beginning of key epoch \( i + 1 \), Bob starts to receive messages encrypted with a different key. Assume that the temporal keys were synchronized in the previous epoch, i.e., \( k^a_i = k^b_i \). Since Bob shares the same model as Alice, he knows the next set of possible keys.

1. Find the set of possible keys from \( k^b_i \): \( \mathcal{N} = \{ n | A(k^b_i, n) > 0 \} \). See figure 2 or section 3.2.2 for details.
2. For each key \( n \in \mathcal{N} \):
   - If \( \psi(x_{i+1}, n) = 1 \), then assign \( k^b_{i+1} = n \) and halt.
   - Else continue checking other keys.

Under our assumptions of epoch synchrony and correctly functioning integrity checks, Bob and Alice will remain in key synchrony, i.e., \( n_0 = \infty \). We treat the case of imperfect integrity checks in section 6.

3.4 Method Efficiency

We now consider the communication, computation, and memory requirements of this scheme.

**Communication:** Aside from the initial synchronization of Markov models, there are no explicit key replacement messages sent between Alice and Bob.

We have also assumed that Alice and Bob remain in synchrony so that they know when to replace their keys. In typical networks, synchrony may already be maintained so that this requirement adds little or no overhead. Alternatively, if the integrity check works perfectly, Bob no longer needs to know a priori when Alice changes her key. Alice can change the temporal key at will and Bob will be able to detect the change and search for the new key.

**Computation:** The transmitter only needs to select a key from the set of \( d \) possible future keys. The receiver, however, needs to check the set of possible keys until the correct one is found. Thus, he needs to perform up to \( d \) decryptions and integrity checks. Since the next key is chosen with equal probability from the set, on average the receiver will perform \( d/2 \) decryptions and integrity checks.

Since the possible key transitions from the current key are not stored in memory, we must consider the computation costs required to generate them. As we discuss in section 4, for security purposes, we require the use of cryptographically secure PRNGs (CSPRNGs),
which generally have higher complexity than non-CS PRNGs. For example, the Blum Blum Shub CSPRNG has a security proof based on the hardness of integer factorization, but has complexity equal to RSA (13). Lower complexity CSPRNGs such as Yarrow have been shown through practice to be resistant to attack, but no such proofs of security exist for them (14).

Memory: We have shown in section 3.2.1 that it is not necessary (or possible in most instances) to store the entire set of Markov models in memory. In particular, we show that Alice and Bob only need to store the session key and the current temporal key, since the set of possible future keys can be computed directly from the model. The minimum storage requirement is therefore \( \log_2(L) + \log_2(K) \) bits.

4. Security of the Proposed Method

In this section, we show that the proposed method has perfect forward secrecy and is resistant to known-key attacks. Further, little information about the session key is revealed by the replacements. That is, we show that the following properties about the codebook \( \Lambda \) hold:

1. \( H(k_j|l, k_i) \cong H(K) \) for \( j < i \)
2. \( H(k_{i+1}|k_i) \cong H(K) \)
3. \( H(l|k_i) \cong H(\Lambda) \)

where \( K \) is the collection of temporal keys, \( \Lambda \) is the collection of Markov models, and \( H(\cdot) \) is Shannon entropy defined on a random variable \( X \) as

\[
H(X) = \sum_x -p(x) \log_2 p(x)
\]  

(12)

The properties state that (1) compromise of the session key does not expose the previous temporal keys, and that compromise of the current temporal key reveals little information about (2) subsequent temporal keys or (3) the session key (i.e., the Markov model in use).

To ensure keys with high equivocation, the transition probabilities of the Markov models should be uniformly distributed. Since the models are pseudo-randomly generated, the PRNG output should appear to be statistically random, i.e., nearly uniformly distributed so that there is little skew or bias. For this reason, for simulations we use the Mersenne Twister PRNG, whose output has good statistical properties (15).
However, we should note that PRNGs that pass statistical tests are not necessarily sufficient for security purposes. For example, though the digits of the scalar constant $\pi$ may pass any statistical test for randomness, they are predictable and hence exploitable by any reasonably capable adversary. Thus, the PRNG needs to not only produce seemingly random output but also be unpredictable to the adversary.

Finally, we show that the entropy of the generated key is limited to the branching factor $d$. In the ideal case, the entropy would be $H(K)$, but the proposed method trades the key entropy for computation costs. However, as is shown in the sequel, the method has good equivocation properties that make it resistant to attack.

### 4.1 Forward Secrecy

Suppose that Eve is able to discover the session key $l$ as well as the temporal key $k_i^a = k_i^b$. Is she able to recover the previous temporal keys $\{k_1, \ldots, k_{i-1}\}$? While the forward transitions are easy to calculate, by the nature of the construction (section 3.2.2), it is not as easy to find the backward transitions. When Eve does not know about the structure of the Markov model in use, she has no choice but to brute-force search the keyspace to find the possible previous keys. In other words, the key equivocation is near maximal

$$H(k_j | l, k_i) \approx H(K) \text{ for } j < i$$

since Eve gains no information about the previous keys. This is the ideal case in terms of security since it offers perfect forward security. Note that even Alice and Bob, who know which model they are using, have no advantage in specifying the structure of the model since they do not store it entirely in memory. Again, we emphasize that this property relies heavily on the unpredictability of the PRNG.

Since the models are (pseudo-)randomly generated, we rely on the security afforded by the underlying PRNG. If Eve is able to discover the structure of the PRNG, she is potentially able to discover the prior temporal keys. Thus, the forward security of the proposed key replacement method relies on the unpredictability of the PRNG. CSPRNGs are designed to be unpredictable at the cost of increased computation compared to non-CS PRNGs.

### 4.2 Entropy of Next Temporal Key

Given a model and the current temporal key, there are $d$ candidates for the next temporal key. Over all $L$ possible models that are generated from the same PRNG, there are therefore $dL$ candidates uniformly distributed over the $K$ possible keys. The probability of transitioning from key $m$ to key $n$ is therefore

$$\frac{1}{dL} \sum_i A^l(m, n) = \frac{1}{dL} |A(m, n)|$$

12
The entropy is therefore

\[ H(k_{i+1}|k_i = m) = \sum_n h\left( \frac{1}{dL}|A(m, n)| \right) \]

where

\[ h(y) = -y \log_2(y) \]

(15)

(16)

Since the keys are chosen uniformly over each \( A \), \( P(|A(m, n)| = x) \) is approximated by the Poisson distribution

\[ P(|A(m, n)| = x) = f(x, \bar{x}) \]

\[ = \frac{\bar{x}^x e^{-\bar{x}}}{x!} \]

(17)

(18)

where \( \bar{x} \) is the expected number of occurrences. In our case, \( \bar{x} = dL/K \).

The entropy of the next key can thus be approximated

\[ H(k_{i+1}|k_i = m) = \sum_x E[|A(m, n) = x|] h\left( \frac{x}{dL} \right) \]

\[ = \sum_x K f(x, \bar{x}) h\left( \frac{x}{dL} \right) \]

(19)

Figure 3 shows that the entropy is close to the maximum when the branching factor \( d \) is high and the number of models \( L \) is high. The critical point is that \( dL \) must be greater than \( K \); this ensures that over all the models the possible keys are sufficiently random. Note that with sufficiently many models, the branching factor contributes only a small amount of entropy.

A subtle but crucial point that arises is the question of key reachability. Namely, how do we guarantee that given a particular temporal key, the set of possible subsequent keys is large? It is certainly possible for temporal keys to traverse only a small space, which leads to poor security since subsequent keys may be easily recovered. We show in section 5 that with high probability, the set of possible subsequent keys for any given temporal key is large.

4.3 Entropy of the Session Key

The current temporal key should give little information about the session key, or equivalently, which model \( \lambda \) is being used. From section 5, we know that the giant connected component (GCC) \( G \) has size \( O(K) \) and that the number of non-zero stationary probabilities \( \mu_i \) are also \( O(K) \). For large \( d \), we can approximate \( |G| \approx K \).

The temporal key sequence generated using the model forms a Markov chain. Assume that the Markov chain is in steady state. Let the stationary probability of key \( i \) under model \( l \)
Figure 3. Entropy of next key given the current key. The Markov model is not known to the adversary. $K = 2^{64}$.

be $\mu^t_i$. Then the entropy of the model given the current temporal key $k_i$ is

$$H(l|k_i) = \sum_l h\left(\frac{\mu^t_i}{\sum_l \mu^t_i}\right)$$  \hspace{1cm} (20)$$

We note from experiment that the stationary probabilities are well approximated by a Rayleigh distribution when $d$ is small and a normal distribution when $d$ is large (figures 4 and 5, respectively). In the experiment, we assumed $K = L = 1024$ and used the Mersenne Twister as the PRNG.

Figure 6 shows that the model entropy is close to the maximum when the branching probability is high and the number of models $L$ is high. Increasing the branching factor improves the model entropy.
Figure 4. Distribution of stationary probabilities is well approximated with Rayleigh distribution for small $d$.

Figure 5. Distribution of stationary probabilities is well approximated with Gaussian distribution for large $d$. 
4.4 Entropy Rate

Since the GCC is strongly connected, it is irreducible. With high probability, random
digraphs are also aperiodic. An irreducible and aperiodic Markov chain converges to its
unique stationary distribution $\mu$ (16), and the resulting entropy rate is

$$H(K) = - \sum_{m,n \in \mathcal{G}} \mu_m A_{mn} \log A_{mn} \leq \log d \tag{21}$$

with equality when a transition between keys $m$ and $n$ implies that $A_{mn} = 1/d$. Thus,
entropy rate is maximized when future keys are equiprobable.

In comparison, in section 4.2, we showed that when the model is not known, the entropy of
the next key was shown to be high, near the entropy of the keyspace $\mathcal{K}$.

Having a higher entropy rate is beneficial for security since a single model can generate
many unique temporal key sequences. (Consider the multiplicity of paths that arise when $d$
is increased from 1.) This, in turn, makes it more difficult for the adversary to determine
which model is being used. She may try to use the Baum-Welch algorithm to determine
the underlying model, but the estimated parameters are not accurate unless the number of
observations is very high with respect to size of the state space (17). With a large
keyspace, it will take an infeasibly long time to make sufficient observations of each key.
5. Random Markov Model: Structure

Since we are using the Markov models for temporal key replacement, we are interested in the structure of the pseudo-randomly generated model. Though the models are deterministic given the particular PRNG used for generation, we assume for analysis that they are statistically random and unpredictable (as discussed in section 4). Thus, without fully specifying the model, which is infeasible for realistic key sizes, the structure of the model is apparently random. We are therefore unable to guarantee certain properties of the models, but we can make probabilistic statements. We say that an event occurs with high probability when it occurs with probability 1 as \( K \) increases without bound.

In this section, we show that for any temporal key, the set of possible subsequent keys is large. This property makes it infeasible for the adversary, given reasonable constraints on her ability to perform a successful brute-force attack (i.e., test every key). In other words, we never want to be in a situation where choosing a particular key limits the choices of subsequent temporal keys.

In terms of graph theory, the reachable subspace for most keys in \( K \) should be large, that is, \( O(K) \). A key \( v \) is reachable from \( u \) if there exists a (directed) path from \( u \) to \( v \): \( u \rightarrow v \). The reachable subspace for a key \( u \) is the set of all \( v \) for which \( u \rightarrow v \).

First, we introduce the concept of strongly connected components. We use results from graph theory to show that the size of a single GCC depends on the branching factor \( d \) \( (18) \). Finally, we show that with probability 1, (a) all keys can reach the GCC and (b) no keys leave the GCC. That is, the random Markov models are guaranteed to give highly random key replacements.

5.1 Size of the GCC

We define some terms to facilitate the following discussion.

Definition 3 A digraph \( S \) is a strongly connected when there exists a directed path between any randomly chosen pair of vertices \( u, v \in S \):

\[
\begin{align*}
  u & \rightarrow v \\
  v & \rightarrow u
\end{align*}
\]

Definition 4 The strongly connected components (SCCs) of a digraph are the maximal strongly connected subgraphs. For a given digraph, the SCCs may be identified using efficient algorithms such as Tarjan’s algorithm \( (19) \) or Gabow’s algorithm \( (20) \).
**Definition 5** When the size of a SCC reaches $O(K)$, it is typically referred to as the GCC since it dominates the other SCCs in size.

The significance of the GCC is that for any given key in the GCC, it can reach any other key of the GCC given enough transitions. When the GCC is large, this implies that there are many keys that can be chosen in the future, which is good for security.

We outline the procedure of finding the GCC size and then give the results. We need the following definitions to proceed. We outline the procedure of finding the GCC size and then give the results. We need the following definitions to proceed. The **fan-in** of a node $v$ is the set of vertices $u$ for which $u \rightarrow v$.

The **fan-out** of a node $u$ is the set of nodes $v$ for which $u \rightarrow v$. The fan-out (or fan-in) of a vertex is large when its size is $O(K)$. Let $L^+$ be the set of vertices with a large fan-out, and let $L^-$ be the set of vertices with a large fan-in.

Intuitively, when a node $u$ has a large fan-out and a distinct node $v \neq u$ has a large fan-in, the path $u \rightarrow v$ exists with high probability. Thus, nodes that have both large fan-in and large fan-out are likely to be connected (18). We highlight the relevant results below.

Let $\pi^-$ (resp., $\pi^+$) be the probability that a randomly chosen vertex has a large fan-in (resp., large fan-out). It follows that $|L^-| = \pi^- K$ and $|L^+| = \pi^+ K$. They are the smallest non-negative solutions of

\[
1 - \pi^- = \sum_i p^-_i (1 - \pi^-)^i
\]

\[
1 - \pi^+ = \sum_i p^+_i (1 - \pi^+)^i
\]

where $p^-_i$ (resp., $p^+_i$) is the probability that a key has exactly $i$ incoming (resp., outgoing) transitions. These probabilities are calculated as

\[
p^-_i = \binom{K}{i} p^i (1 - p)^{K-i}
\]

\[
p^+_i = \begin{cases} 1 & i = d \\ 0 & \text{otherwise} \end{cases}
\]

where $p$ is the probability that there exists a transition between a randomly chosen pair of current and next keys. Since each vertex has constant out-degree $d$, we have $p = d/K$, and so the in-degree distribution is given by the binomial probability mass function with parameter $p$.

When $d > 1$, $\pi^-$ has a unique solution in $(0, 1)$, and $\pi^+ = 1$. In other words, a positive fraction of vertices have large fan-in while all vertices have large fan-out (i.e., $|L^+| = K$).
Based on the argument above, the size of the GCC is approximately

$$|\mathcal{G}| \approx |L^- \cap L^+|$$

$$\approx |L^-| + |L^+| - |L^- \cup L^+|$$

$$\approx (\pi^+ + \pi^- - (1 - \psi)) K$$

where

$$\psi = \sum_{i,j} p_{ij}(1 - \pi^-)^i(1 - \pi^+)^j$$

$$= 0$$

since $\pi^+ = 1$. Thus, the GCC $\mathcal{G}$ is unique with size

$$|\mathcal{G}| \approx \pi^- K$$

with probability approaching 1 as $K \uparrow \infty$.

Table 1 shows the theoretical and observed size of the GCC for various branching factors. For each value of $d$, 100 matrices of size $K = 2^{10}$ were generated using the Mersenne Twister PRNG. The size of the GCC was found using Tarjan’s algorithm and averaged over each realization. Shown in the table is the ratio of GCC size to $K$. The theoretical GCC size matches very well with the empirical evidence. Clearly, increasing $d$ increases the proportion of the GCC, though the gains diminish after $d = 4$.

<table>
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<th>Branching factor</th>
<th>GCC Proportion</th>
<th>Penalty (bits)</th>
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<td>.9990</td>
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<tr>
<td>8</td>
<td>.9997</td>
<td>.9997</td>
</tr>
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</table>

When the size of the GCC is less than $K$, the size of the reachable subspace is diminished. In bits, we say that the penalty is

$$\text{Penalty} = -\log_2(\frac{|\mathcal{G}|}{K})$$

For example, if the GCC has size $2^9$ but the keyspace has size $2^{10}$, then the penalty is 1 bit. Thus, the keys that are traversed offer the security of a 9-bit key instead of a 10-bit key.

Note the significant decrease in penalty as the branching factor is increased from 2 to 4. We observe diminishing improvements for larger branching factors.
5.2 Reachability of the GCC

Since the GCC $G$ is large, any key $k \in G$ has a reachable subspace with size $O(K)$ by definition. However, what about those keys that are not in $G$? In order to guarantee keys that traverse a large space, we need to show that with high probability

- regardless of initial key, the key replacement algorithm eventually chooses members of the GCC, and
- if the current temporal key is in the GCC, future replacement keys will remain in the GCC.

First, observe that when a key leaves the GCC, it does not have a path that returns to the GCC. To see why, suppose that the path $G \rightarrow v$ exists, where $v \notin G$. If a path $v \rightarrow G$ exists, then since $G \rightarrow v$ this implies that $v \in G$, which is a contradiction. In other words, when the replacement key sequence transitions outside of the GCC, it can never return. Therefore, we need to show that once a key from the GCC is chosen, keys outside the GCC are never chosen in the future.

Let us term the keys that are not in $G$ as external. Let $G^-$ be the set of external keys that have a path to $G$ and let $G^+$ be the set of external keys that are reachable from $G$, i.e.,

$$G^- = \{u|u \leadsto G\} \quad (35)$$
$$G^+ = \{v|G \leadsto v\} \quad (36)$$

The resulting set $B = G^- \cup G \cup G^+$ forms a bowtie digraph as shown in figure 7. The bows of the graph are formed by two wings: $G^+ = L^+ \cap \overline{G^-}$ and $G^- = \overline{L^+} \cap L^-$. Recall that $|L^+| = K$ and hence $L^+ = K$. Hence $B = K$, i.e., the bowtie graph encompasses all vertices in the space. It follows that $\overline{L^+} = \emptyset$ and therefore $G^- = \emptyset$. Therefore, any randomly chosen key is either in $G^+$ or $G$.

The structure of $B$ yields the following properties:

1. If a key is not in $G$, then it is in $G^+$. Therefore, with probability 1, the current state will eventually be in $G$. With probability approaching 1 as $K \uparrow \infty$, any randomly chosen key will enter the GCC.

2. Once a key is in the GCC, it will not depart since with probability approaching 1 as $K \uparrow \infty$, $|G^-| = 0$. 

---

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Figure 7. An example bowtie digraph connected to the giant connected component $\mathcal{G}$. $\mathcal{G}^+$ leads into $\mathcal{G}$, $\mathcal{G}^-$ emanates from $\mathcal{G}$.

In terms of temporal keys, the structure of the random Markov model guarantees that each temporal key can reach a large subset ($O(K)$) of the keyspace. Therefore, the temporal keys that will be generated from our key exchange algorithm traverse a large space thus making the task of the adversary difficult.

6. Extension: Imperfect Key Recovery

In section 3, we assumed that as long as one of the keys Bob tests is the correct key, he is able to determine the correct key without error. This is a good approximation in most applications, but in this section we determine the effects of detection error on the proposed key replacement method.

Suppose that the ciphertext $x_i$ has been encrypted with key $k_i$ as in equation 1. When we test a single key $m$, there are two cases where the key recovery fails.

1. Missed detection: the correct key is tested ($m = k_i$) but fails the check with probability $1 - p > 0$:

$$\psi(x_i, m = k_i) = \begin{cases} 0 \text{ w.p. } 1 - p \\ 1 \text{ w.p. } p \end{cases}$$ (37)

2. False alarm: the wrong key is tested ($m \neq k_i$) but passes the check with probability
\(\alpha > 0:\)

\[
\psi(x_i, m \neq k_i) = \begin{cases} 
0 \text{ w.p. } 1 - \alpha \\
1 \text{ w.p. } \alpha 
\end{cases}
\] (38)

Recall that the recovery performed by Bob (section 3.3) checks the validity of \(d\) keys. We assume that the integrity checks have independent outcomes. Considering a set of \(d\) keys where exactly one is correct, there are four possible types of outcomes.

1. The correct key passes the integrity check (all others fail). This occurs with probability

\[
Pr[\text{Case 1}] = p(1 - \alpha)^{d-1}
\] (39)

2. The wrong key passes the integrity check (all others fail). This occurs with probability

\[
Pr[\text{Case 2}] = (d - 1)(1 - p)\alpha(1 - \alpha)^{d-2}
\] (40)

3. No keys pass the integrity check. This occurs with probability

\[
Pr[\text{Case 3}] = (1 - p)(1 - \alpha)^{d-1}
\] (41)

4. Multiple keys pass the integrity check. This occurs with probability

\[
Pr[\text{Case 4}] = 1 - Pr[\text{Case 1, 2, or 3}]
\] (42)

Looking ahead to section 6.2, the probability of a correct detection (\(Pr[\text{Case 1}]\)) needs to be sufficiently high, otherwise Alice and Bob will lose synchrony quickly. In the following section, we modify the recovery algorithm to improve the detection probability in the midst of errors.

### 6.1 Extended Recovery Algorithm

In general, a key is used to encrypt multiple messages during the same epoch. Rather than determining the replacement key after a single message, consider how \(C\) messages can be used to make the decision. For the key epoch \(i\), we denote the encrypted messages by \(x_1^i, x_2^i, \ldots\)

We assume that the number of times each key passes the integrity check are independent. Bob tallies the number of times a key passes the check over the \(C\) messages, and selects the key that passed the most times. We assume that \(k_i^a = k_i^b\) and \(\lambda^b = \lambda^a\) so that Bob knows the transition probabilities to the next key.

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1. Find the set of possible keys from \( k_i^b \): \( \mathcal{N} = \{ n | A(k_i^b, n) > 0 \} \).

2. For each key \( n \in \mathcal{N} \):

\[
T[n] = \sum_{c=1}^{C} \psi(x_{i+1}^c, n) \quad (43)
\]

3. Select \( k_{i+1}^b = \arg \max_n T[n] \)

The probability that the correct key will be detected \( c \) times out of \( C \) is given by the binomial probability \( B(c, C, p) \), where \( p \) is the probability of the correct key passing the integrity check. Similarly, for the incorrect keys the probability is \( B(c, C, \alpha) \), where \( \alpha \) is the probability of an incorrect key passing the integrity check. Since the trials have independent outcomes, the probability that Bob chooses the correct key is given by

\[
\hat{p} = Pr[k_{i+1}^b = k_{i+1}^a] = \sum_{c=1}^{C} B(c, C, p) \left( \sum_{d=0}^{c-1} B(d, C, \alpha) \right)^{d-1} \quad (45)
\]

Aside from the detection and false alarm probabilities \( (p, \alpha, \text{ respectively}) \), the number of messages \( C \) determines the detection probability \( \hat{p} \) of the correct key. Figure 8 shows that the probability of choosing the wrong key falls exponentially as \( C \) increases. Further, the test does not need to consider large \( C \) when the detection probability \( p \) is high.
Figure 8. Probability of choosing the incorrect key for various raw detection key probabilities \( p \) when \( \alpha = 10^{-7} \). Extending the key replacement over multiple messages encrypted with the same key improves the detection probability. Lower \( p \) require more observations for good detection probability.

6.2 Synchronization Performance

The probability that Bob chooses the incorrect key is \( \varepsilon = 1 - \bar{p} \). Thus, the probability that Alice and Bob lose synchrony at epoch \( n_0 \) is

\[
Pr(\text{Lost at } n_0) = \varepsilon (1 - \varepsilon)^{n_0 - 1}
\]  

(46)

We are interested in the case when Alice and Bob maintain synchrony for at least \( n_0 \) with a certain probability. That is,

\[
Pr(n_0 > n) = \sum_{n<n_0} Pr(\text{Lost at } n_0)
\]  

(47)

\[
= 1 - (1 - \varepsilon)^{n-1}
\]  

(48)

\[
n = \frac{\log(1 - Pr(n_0 > n))}{\log(1 - \varepsilon)}
\]  

(49)

For example, we calculate that when \( \varepsilon = 10^{-4} \), then with probability 99.99% Alice and Bob remain synchronized for at least \( 9.2 \times 10^4 \) keys. Figure 9 shows the number of key transitions before failure for various confidence levels.
6.3 Extension Efficiency

When the recovery of the key is extended for $C$ messages, the number of computations and memory requirements necessarily increase.

*Communication:* As in section 3, no explicit key replacement messages are exchanged. However, there is an increased delay since the key decision requires the receipt of $C > 1$ messages.

*Computation:* Since the computations are identical for each message, the considering keys over multiple messages times increases the computations by a factor of $C$. The final step of selecting the key with the largest score requires negligible computation.

The cost of running the PRNG does not change and is the same as in section 3.4.

*Memory:* The set of possible keys remains constant over the duration of the test, so there is no additional cost. However, there is the need to keep the tally of how many times each key passes the integrity checks. This requires $\log_2(C)$ bits per key, or $d\log_2(C)$ bits in total. Note that there was no need to keep score when the integrity check is perfect because exactly one key would satisfy the integrity check.
7. Related Work

We give a characterization of a few approaches towards key replacement and highlight their differences with the proposed method.

One of the most trivial rekeying strategies has Alice and Bob using their session key to seed a PRNG. Periodically, they update their keys by taking the next $n$ digits as the new temporal key. While this requires no extra communication, the security of this method is weak—the new temporal keys have no more randomness than the session key used to seed the PRNG. Once the PRNG is seeded, the sequence of temporal keys is completely deterministic and hence vulnerable to attack. In fact, this rekeying strategy may be viewed as a degenerate case of the proposed method with branching factor $d = 1$. For comparison, the proposed method (with $d > 1$) adds key entropy during each rekey because of the randomization (section 4.4).

A stronger method is to use a one-way function with a nonce to generate the next key, e.g., $k_{i+1} = F(x, k_i)$ with $k_i$ the current key, $x$ the nonce, and $F(\cdot)$ the one-way function. In order to recover this key, the receiver needs knowledge of the nonce—it can be encrypted with the temporal key and transmitted. A weakness with this approach is that the discovery of a temporal key reveals all subsequent keys. This also requires some bandwidth to transmit the nonce. The proposed method uses Markov models to restrict the possible nonces in order to avoid the use of nonces while also preventing subsequent keys from being revealed.

Instead of using the session key to encrypt all the temporal keys, the idea behind hash chains (21) is to derive past keys from future keys. In particular, the current temporal key $k_i$ is calculated using the next key $k_{i+1}$ and a one-way hash function $F(\cdot)$, i.e., $k_i = F(k_{i+1})$. Alice and Bob generate a chain of hash values derived from the same initial key $k_n$, and begin to use the key $k_0$. To replace the key, they simply use the next key $k_1$. However, after $n$ key replacements Alice and Bob need to resynchronize and generate another hash chain. This is not a very big problem, however, since hash chains can be computed very efficiently (22). A significant weakness of hash chains is that there is no forward secrecy. Once a key is compromised, the revelation of all past keys is trivial due to their deterministic dependencies. While this property makes the use hash chains less than ideal for key replacement, hash chains have found interesting applications in routing protocols in ad hoc networks (23).

---

‡A function is one-way when it is easy (feasible) to compute but hard (infeasible, given resource constraints) to invert.
The “sign and MAC” (SIGMA) approach encompasses a large family of key exchange protocols that build upon the well-known Diffie-Helman (DH) key agreement protocol (8, 9). Careful combinations of digital signatures and message authentication codes (MACs) are used to provide the security basis for signature-based authenticated key exchange using DH protocols (e.g., IKE [24]). Generally these protocols require at least three messages for both parties to contribute entropy towards the new key, bind identities with signatures, and authenticate each other. Each message is accompanied by the corresponding computation, which can be expensive; modular exponentiation is not as cheap as symmetric encryption or decryption.

Another well-known protocol is Kerberos (10) (based on the Needham-Shroeder shared-key protocol [25]), which uses a trusted authentication server to facilitate key exchange. The authentication server has session keys shared individually with Alice and Bob and creates temporal keys for them to use among themselves. All the encryptions are symmetric and are therefore cheap, but this protocol requires the exchange of more messages because Alice and Bob need to interact with the authentication server. The biggest caveat, of course, is the existence and cooperation of such an authentication server.

A summary of the requirements of the key replacement methods are shown in table 2. Note that there is no method that is simultaneously low-complexity, independent of third parties, and secure. The proposed key replacement method is conceptually simple and its security depends on randomness of the underlying CSPRNG. The choice of CSPRNG varies the computational requirements of the method.

Table 2. Comparison.

<table>
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<th>Method</th>
<th>No. of Messages</th>
<th>Computation Cost</th>
<th>Third Party?</th>
<th>Security</th>
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<td>Low</td>
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<td>Kerberos</td>
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<td>Low</td>
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<td>High</td>
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<td>0</td>
<td>Variable</td>
<td>No</td>
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</tbody>
</table>
8. Conclusion

We have introduced a novel rekeying method that exploits the randomness of Markov models to efficiently provide fresh keys to the users. The method is shown to generate highly random symmetric keys while remaining lightweight in terms of communication and storage costs. The security of the method depends on the underlying CSPRNG and generally is improved at the cost of increased computational requirements. We have also demonstrated that the proposed method has perfect forward secrecy as well as resistance to known-key attacks. Finally, we note that the usefulness of the method is not restricted to keys, but to any variable that is changed in a synchronous manner. For example, this method can apply to frequency-hopped communications systems to vary the hop set ordering.
References


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