An Experimental Exploration of the Impact of Sensor-Level Packet Loss on Network Intrusion Detection

by Sidney C Smith and Robert J Hammell II

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In this report we consider the problem of sensor-level packet loss (SLPL) as it applies to network intrusion detection. We explore 2 research questions: 1) Is there sufficient regularity in SLPL to allow an algorithm to be developed to model it? and 2) Is the impact of SLPL on network intrusion detection performance sufficiently regular to allow a formula to be developed that will accurately predict the effect? We developed and validated the Pcapreplay program, which allowed us to characterize the manifestation of SLPL. We conducted experiments using Pcapreplay and Snort to explore the impact of SLPL. We graphed and analyzed this impact against our previous theoretical work. We conducted experiments using Pcapreplay and Snort to measure the impact on network intrusion detection. We graphed the alert loss rate against the packet loss rate. We compared these graphs to our previous theoretical work. We used nonlinear regression analysis to produce a formula with r-squared and reduced chi-squared values close enough to 1 for us to answer both of our research questions in the affirmative.

packet loss, network intrusion detection, software, Snort, Tcpdump, Pcapreplay
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1. Introduction

As we consider the impact of sensor-level packet loss (SLPL) on network intrusion detection (NID), we observe that NID depends upon the sensor being able to see the traffic between the adversary and the target. General packet loss is very common on the Internet. The Transmission Control Protocol is specifically designed to account for general packet loss and uses it as a barometer to gauge the available bandwidth of a connection.¹ In this report we are not interested in general packet loss because those packets cannot cause a compromise since they will never reach the target. We are interested in what we call detection-relevant packet loss (DRPL). DRPL occurs when packets reach the target but fail to reach the sensor software for analysis. Since the sensor cannot detect what it cannot see, DRPL must have a negative impact on the sensor’s ability to detect malicious activity. Based upon the large amount of work that has been done to reduce or eliminate DRPL on NID, we infer that the negative impact of DRPL on NID is well known. This report is part of a larger effort to understand, predict, and model the impact of DRPL on NID. In our previous theoretical work,² we divided DRPL into network, host, and sensor levels. In this report, we will focus on DRPL at the sensor level. SLPL is defined as any packets that are processed by the host operating system but are not processed by the analysis software.

The focus of this report is to answer 2 research questions concerning the manifestation of SLPL and the impact of SLPL on NID: 1) Is there sufficient regularity in SLPL to allow an algorithm to be developed to model it? and 2) Is the impact of SLPL on NID performance sufficiently regular to allow a formula to be developed that will accurately predict the effect? We discovered that the manifestation of SLPL is not random but is very similar to the capped algorithm of the packet dropper we developed in our previous theoretical work.² We also discovered that the impact of SLPL is not random but is very similar to both the results of the capped-by-packet algorithm of the packet dropper and a sigmoid function. When we used regression techniques to compare these algorithms, each of them had $R^2$ and $\chi^2_v$ values very close to 1. These discoveries allow us to answer both of our research questions in the affirmative.

In Section 2 we provide an overview of the existing research, which is heavily focused upon eliminating packet loss at the sensor level. In Section 3 we discuss the Pcapreplay program, which we developed to explore SLPL, the dataset that we
used in these experiments, the experiment to characterize SLPL, and the experiment to measure the impact of SLPL. Section 4 describes the results of our experiments and our regression analysis of these results, and Section 5 summarizes our results and discusses future work.

2. Background

In previous research we considered the theoretical impact of packet loss on NID. We divided the potential for packet loss among the network, host, and sensor level. We also defined network-level packet loss as any packet that reaches the target but fails to reach the network segment where the sensor is located. Additionally, we defined host-level packet loss as any packet that reaches the network interface of the sensor but is not presented to the analysis software. SLPL is defined as any packet that is presented to the analysis software but is not processed. The various level of packet loss may be seen in Fig. 1. SLPL is represented by bit bucket C.

![Detection-relevant packet loss diagram](image)

**Fig. 1 Detection-relevant packet loss diagram**
We constructed the packet dropper, which abridges datasets according to several different algorithms we implemented to emulate our theories about how packets may be lost. We also visualized the characterization of this packet loss by graphing the network traffic from 2.5 min of traffic from the 2009 Cyber Defense Exercise (CDX) dataset, which we describe in detail in Section 3.2, as it was abridged at 25% packet loss by each of the packet dropping algorithms.

Although work has been done to reduce or eliminate packet loss, there has been little work done to understand and model packet loss and its impact on NID. We were able to glean several insights into packet loss from the work done to reduce or eliminate packet loss. In Schaelicke and Freeland’s work on characterizing the sources and remedies for packet loss in NID, they obtained some improvements in packet loss rates by increasing the level of optimization employed in the compiler. They also found that significant improvements in packet loss could also be achieved by pruning the sensor rule set. Additionally, Salah, in his work on improving snort performance under Linux, discovered that setting the netdev_budget, which is a kernel configuration parameter in the New Application Programming Interface, to a low number greatly decreases packet loss. He concluded that this occurred primarily because pulling packets from the network and analyzing the packets are bound by available central processing unit (CPU) cycles and not buffer memory. Allocating the bulk of the CPU time to the sensor application enables the system to process more packets. Additionally, the packets that are dropped are dropped very early in the process, preventing CPU cycles from being wasted processing packets that will only be dropped later. Furthermore, in their work on hash-based load balancing, Kim et al. successfully employed multiprocessing techniques to increase the throughput of the sensor and reduce packet loss. In their work on achieving flow-level controllability in NID, Song et al. point to the software crash as yet another cause of packet loss. Finally, in their work on adapting the intrusion detection system model to load characteristics under Internet Protocol version 6, Wei et al. proposed breaking the detection task into 3 units: the Data Acquisition Unit, the Adapt Load Characteristic Analysis Unit, and the Collaborative Analysis and Control Center.

Revisiting bit bucket C in Fig. 1, we expected that the resource consumption of the sensor application itself will contribute the greatest component of packet loss at this level. We theorized that we could simulate this effect through a cyclic function,
such as a sine wave that would model a process gathering resources, performing its task, and releasing the resources.  

3. Approach

Our approach to answering our research questions requires several building blocks. First, we will need some method to simulate and isolate SLPL; we will use the Pcapreplay program developed for this effort, as described in Section 3.1. We will also need NID software for our experiment; we will use Snort for this purpose. Last, we will need network capture data in Tcpdump format; we will use portions of the CDX 2009 dataset, described in greater detail in Section 3.2, for this purpose. We will compare this data to data generated using the packet dropper we developed in a previous effort. In addition to the tools described above, our approach to answering our first research question is detailed in Section 3.3, and our approach to answering our second research question is detailed in Section 3.4.

3.1 Pcapreplay

Answering our research questions requires that we isolate and measure SLPL. If we configured Snort to read from the network stack, it would be impossible to know whether the packets were dropped because the network stack could not process them or because Snort could not process them in time. To isolate the sensor layer, we will pipe packets in Tcpdump format to Snort on standard input. Snort will report the number of packets that it dropped; however, that will provide no insight into which packets were dropped. Snort will either capture packets or it will analyze packets, but it will not do both. To gain insight into how these packets are lost, we will need to have some way to record which packets are lost. To do this, we have written the Pcapreplay tool, which reads a file in Tcpdump format using Libpcap and writes the packets in Tcpdump format at any multiple of the original speed. Packets that cannot be written in time are written to a bit bucket file. We can then analyze the bit bucket file to gain insight into how the packets are lost in order to determine if there is sufficient regularity in SLPL to allow an algorithm to be developed to model it. We understand that in many ways this is similar to the Tcpreplay command, which will take packets from a file saved in Tcpdump format and replay them on the network at any multiple of the original captured speed.

Algorithm 1 provides the pseudo code for the core of the Pcapreplay application. The trickiest part of this algorithm is the fudge factor, which was included because
the library functions sleep\(^{15}\) and usleep\(^{16}\) are guaranteed to sleep for the specified time; however, they may oversleep. We added the fudge factor to account for the system oversleeping.

**Algorithm 1** Core Pcapreplay algorithm

**Require:** fileStartTime = 0

while get next packet do

    fileTime ← packetTime
    currentTime ← gettimeofday()

    if fileStartTime = 0 then
        fileStartTime ← fileTime
        startTime ← currentTime
        elapseStartTime ← currentTime
        initialDifference ← currentTime − fileTime
    end if

    elapseTime ← currentTime − startTime
    effectiveTime ← fileStartTime + elapseTime * accelerator

    if fileTime + fudge ≥ effectiveTime then
        packetsWritten ← packetsWritten + 1
        sleepTime = (fileTime − effectiveTime)/accelerator
        sleep(sleepTime)
        timeNow = gettimeofday()
        newEffectiveTime ← timeNow − initialDifference

        if newEffectiveTime > effectiveTime + sleepTime then
            fudge = newEffectiveTime − effectiveTime − sleepTime
        end if

        writepacket
        flushstream
    end if

else
    packetsDropped ← packetsDropped + 1
    write packet to bit bucket
end if

end while

To validate that Pcapreplay is actually replaying packets at the specified multiple of the original speed, we will use the script described in Algorithm 2 to conduct several trials measuring the time it takes for Pcapreplay to replay 1 h of network traffic. A full description of the capabilities and options of the Pcapreplay tool is in the Appendix. We will use the script described in Algorithm 3 to conduct several trials measuring the time it takes for Tcpreplay to replay the same 1 h of network traffic. If Pcapreplay is working correctly, we should find that the results are very similar. These results may be found in Table 1. Computing the value of \( R^2 \) for
Pcapreplay, using Formula 1, we get 0.9999, which is the same $R^2$ value that we get for Tcpreplay and close enough to 1 for us to conclude that Pcapreplay is actually replaying packets at the correct speed.

\[
R^2 = \frac{SS_{\text{reg}}}{SS_{\text{tot}}} \tag{1}
\]

\[
SS_{\text{reg}} = \sum_{i=1}^{n} (\hat{y}_i - \bar{y})^2. \tag{2}
\]

\[
SS_{\text{tot}} = \sum_{i=1}^{n} (y_i - \bar{y})^2. \tag{3}
\]

**Algorithm 2** Validate Pcapreplay shell script

```bash
#!/bin/sh
speed=1
while [ $(speed) -lt 2048 ]; do
time
   pcapreplay -x $(speed) -b /dev/null -w /dev/null $*
speed=`expr $(speed) \* 2`
done
```

**Algorithm 3** Validate Tcpreplay shell script

```bash
#!/bin/sh
speed=1
while [ $(speed) -lt 2048 ]; do
time tcpreplay -x $(speed) -i eth1 $*
speed=`expr $(speed) \* 2`
done
```

### 3.2 Dataset

Annually, the National Security Agency/Central Security Service conducts an exercise pitting teams from the military academies of the United States and Canada against teams of professional network specialists to see who can best defend their network.\(^3\) In their paper, “Toward Instrumenting Network Warfare Competitions to Generate Labeled Datasets”, Sangster et al.\(^{11}\) describe their efforts to collect and label traffic from the 2009 competition. We were able to obtain this data from https://www.itoc.usma.edu/research/dataset/.
Table 1 Pcapreplay and Tcpreplay validation values

<table>
<thead>
<tr>
<th>Speed</th>
<th>Expected</th>
<th>Pcapreplay</th>
<th>Tcpreplay</th>
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<tr>
<td>1</td>
<td>3600.000</td>
<td>3564.012</td>
<td>3564.962</td>
</tr>
<tr>
<td>2</td>
<td>1800.000</td>
<td>1781.646</td>
<td>1784.305</td>
</tr>
<tr>
<td>4</td>
<td>900.000</td>
<td>890.749</td>
<td>892.991</td>
</tr>
<tr>
<td>8</td>
<td>450.000</td>
<td>444.901</td>
<td>447.348</td>
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<td>16</td>
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<td>224.431</td>
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<td>32</td>
<td>112.500</td>
<td>111.214</td>
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<td>6.787</td>
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<tr>
<td>1024</td>
<td>3.516</td>
<td>3.457</td>
<td>5.340</td>
</tr>
<tr>
<td>2048</td>
<td>1.758</td>
<td>1.742</td>
<td>3.891</td>
</tr>
</tbody>
</table>

This dataset was chosen because one of the files captured by gator010, 20090421.14.ftrm, contains traffic that is consistent enough for us to be able to see the influence of packet loss on the network traffic. We will be using the same 2.5 min of network traffic that was used in our previous research.\(^2\) This will allow us to compare our experimental results with our previous theoretical results.

### 3.3 Characterizing SLPL

To answer our first research question (Is there sufficient regularity in SLPL to allow an algorithm to be developed to model it?), we will establish the null hypothesis that sensor-level packet loss is sufficiently irregular, as to be effectively considered random. We have plotted the effect of random packet loss on this dataset in Fig. 2. To characterize the sensor-level impact, we will use Pcapreplay to replay the CDX dataset, piping it to Snort version 2.9.3.1 using the community rules set from August 2013. Some trial and error will be necessary to discover the Pcapreplay speed setting that will produce approximately 25% packet loss. We constructed a shell script that would conduct trials starting at 2x, continuing until 32768x in a geometric progression, i.e., \(2^n\), using a shell script like the one shown in Algorithm 4. This script should allow us to quickly discover the correct multiplier to achieve 25% packet loss. Once we discover the appropriate speed factor, we can graph the network traffic in the bucket.pcap file. If the SLPL is random, we should see the abridged traffic line beneath and almost identical to the orginal traffic line. If we see this kind of relationship, we must accept the null hypothesis. If there is some regularity to SLPL, the abridged traffic line will show some difference to the original traffic line beyond
a simple reduction. This may be seen in the graph of the traffic from the sinusoidal dropping algorithm in Fig. 2. If we see this kind of relationship, we must reject the null hypothesis.

![Graph showing packet loss](image)

**Fig. 2** Manifestation of 25% packet loss generated by the packet dropper and measured in packets/second

**Algorithm 4** Shell script to automate repeated runs of Pcapreplay

```bash
#!/bin/sh
X=2
while [ $X -lt 65536 ]; do
    mkdir log $X
    pcapreplay \n        -x \$X\n        -w \n        -L log$Xx/replay.log \n        -b log$Xx/bucket.pcap $* 1
    snort \n        -c ~/rules/etc/snort.conf \n        -r \n        -l log$Xx 2> log$Xx/snort.out
    X=\`expr $X \* 2`\ndone
```

### 3.4 Measuring the Impact of SLPL

To answer our second research question (Is the impact of SLPL on NID performance sufficiently regular to allow a formula to be developed that will accurately
predict the effect?), we will establish the null hypothesis that the impact of sensor level packet loss is sufficiently irregular as to be effectively considered random. In an attempt to prove the null hypothesis, we will run the CDX gator010 data through Pcapreplay at various speeds, piping the output to Snort. We will be able to use the shell script from Algorithm 4 with slight modifications to allow for different progressions based upon the results we see from the initial trial in an attempt to obtain a good spread through the packet loss rate (PLR) domain of 0% to 100%. The replay.log file will contain the PLR, and the snort.out file will contain the number of alerts. A control run of Snort against the dataset without Pcapreplay will tell us the total number of alerts, which we may use to calculate the alert loss rate (ALR). Plotting the PLR versus the ALR will allow us to compare the results against our results from the theoretical exploration.\(^2\) We should be able to use curve fitting and regression analysis techniques to discover a relationship and measure the fit. If we are able to discover a relationship and obtain an \(R^2\) value close to 1, we will reject the null hypothesis and may safely conclude that the impact of SLPL on NID performance is sufficiently regular.

4. Results

We will divide our results according to our research questions. In Section 4.1, we will describe the results of our efforts to observe how packet loss manifests itself at the sensor level. In Section 4.2, we will describe the results of our efforts to observe the impact this packet loss has on NID.

4.1 Sensor-Level Packet Loss Manifestation

When we ran our first trial, as described in Section 3, we discovered a speed setting on our hardware that generated 25% packet loss. In Fig. 3, the blue line represents the original traffic, and the red line represents the traffic abridged by Pcapreplay at 25% packet loss. The traffic pattern does not resemble the random or function-influenced traffic patterns from our previous research,\(^2\) seen in Fig. 2. Instead, it resembles the patterns produced by the capped algorithms of the packet dropper (see Fig. 4 for comparison). In Fig. 4, the blue line represents the original traffic and the red line represents the traffic as abridged by the packet dropper using the capped algorithm.
There is a caveat in that the resources of the system used to conduct the experiments have an impact on the shape of the traffic graph. Fig. 5 demonstrates that as the size of the system increases, the traffic graph flattens. The red line represents the results of the experiment run on desktop-class equipment. This red line shows massive oscillation between an upper and lower bound centered around the cap. The yellow line represents the results of the same experiment run on a small server. Some variance is visible in the yellow line; however, the line is much flatter. The black line,
which shows very little variance, represents the results of the same experiment run on a large server.

We observed another difference between the graphs produced by Pcapreplay and the graphs produced by the packet dropper. The line representing packets per second produced by the packet dropper immediately plateaus at the cap. The line representing packets per second produced by Pcapreplay continues to follow the normal traffic flow until it drops and quickly settles into the cap. These observations have little bearing on the current research; however, they may have significant influence in future work as we attempt to validate the results of the packet dropper.

![Graph showing comparison of packet loss](image)

Fig. 5  Comparison of the manifestations of 25% packet loss generated by Pcapreplay on different hardware and measured in packets/second

### 4.2 Impact on the Performance of NID

We created several versions of the shell script described in Section 3 and executed them to collect 4 trials. Each trial consisted of several runs of Pcapreplay, replaying the CDX dataset described in Section 3.2, piped to snort version 2.9.3.1 using the August 2013 rules set. We were able to collect the number of packets lost from the Pcapreplay log and the number of alerts detected from the output of Snort. A control run of Snort against the dataset without using Pcapreplay revealed that there were 5,218,144 packets in the dataset and 275 alerts. We used this information to compute the PLR and ALR for each run of the various trials. Given the similarity in the manifestation of the packet loss to the capped algorithms of the packet dropper, we expect to find a graph similar to Figs. 6 or 7. Figure 6 is the graph of the PLR
versus the ALR when using the capped-by-packets algorithm of the packet dropper.
Figure 7 is the graph of the PLR versus the ALR when using the capped-by-bits algorithm of the packet dropper. In Fig. 8 we see the experimental results.

![Fig. 6 PLR vs. ALR for CDX gator010 abridged with the capped-by-packets algorithm](image1)

![Fig. 7 PLR vs. ALR for CDX gator010 abridged with the capped-by-bits algorithm](image2)
Notice that the graph generated by the packet dropper using the capped-by-packets algorithm appears to be very similar to our results obtained using Pcapreplay. This confirms Salah’s finding that this process is CPU and not memory bound.\(^5\) In Fig. 9 we have plotted the results on the same graph to show this similarity. If we were to treat the ALR of the packet dropper as the predictor \(\hat{y}\) and the ALR of Pcapreplay as \(y\), we could compute \(R^2\) to determine how well the packet dropper predicts the results of Pcapreplay. This assumes that \(x\) or the PLR is the independent variable, which is the model that we are seeking. The problem is that the true independent variable in the Pcapreplay experiments is the speed multiplier, and PLR is a function of that. This means that we cannot use the complete datasets from these experiments. We must use a subset of the datasets where the PLR values are the same. In Table 2 we see the selected data points, and in Table 3 we see several key values. Using Formula 1 to compute \(R^2\), we get a value of 0.96, which would be close enough to 1 to declare that the packet dropper and Pcapreplay are a good fit if this were a linear regression. Our observation of the graph reveals that this is most likely a nonlinear relationship resembling a sigmoid function (see Fig. 10). Spiess and Neumeyer report that \(R^2\) is inadequate for judging the goodness of fit for nonlinear models.\(^17\) They found that the Akaike Information Criterion (AIC), bias-corrected AIC (\(AIC_c\)), Bayesian Information Criterion (BIC), residual variance (resVar), chi-square (\(\chi^2\)), and reduced chi-squared (\(\chi^2_v\)) were better indicators of goodness of fit for nonlinear regression. These are computed using Formulas 5,
6, 7, 8, 9, and 10, respectively, where $\ln(L)$ is the maximum log-likelihood, $p$ is the number of parameters in the model, and $\sigma^2$ is the variation. Since the packet dropper uses an algorithm rather than a formula, we set $p = 3$ because the algorithm depends upon 3 independent variables. It turns out that the AIC, $AIC_c$, and BIC are very good for comparing the fit to different formulas; however, they do not indicate very much standing alone. The $\chi^2_v$ value may be used to judge the goodness of fit for nonlinear regression, where the closer $\chi^2_v$ is to 1, the better the fit. In this case $\chi^2_v$ is 1.1785, indicating that we have a good fit.

$$\ln (L) = 0.5(-N(\ln 2\pi + 1 - \ln N + \ln \sum_{i=1}^{n} x_i^2)).$$  (4)

$$AIC = 2p - 2\ln (L).$$  (5)

$$AIC_c = AIC + \frac{2p(p + 1)}{n - p - 1}.$$  (6)

$$BIC = p \ln (n) - 2 \ln (L).$$  (7)

$$\text{resVar} = \frac{\text{RSS}}{n - p}.$$  (8)

$$\chi^2 = \sum_{i=1}^{n} \frac{(y_i - f(x_i))^2}{\sigma_i^2}.$$  (9)

$$\chi^2_v = \frac{\chi^2}{v}.$$  (10)
### Table 2 Packet dropper and Pcapreplay comparison values

<table>
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<th>PLR</th>
<th>PD ALR</th>
<th>PR ALR</th>
<th>e</th>
<th>(e^2)</th>
<th>((y - \hat{y})^2)</th>
<th>((\hat{y} - \bar{y})^2)</th>
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<td>31.02</td>
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<td>54.55</td>
<td>79.27</td>
<td>24.73</td>
<td>611.44</td>
<td>1580.16</td>
<td>225.72</td>
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<td>69.09</td>
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<td>23.27</td>
<td>541.62</td>
<td>2792.29</td>
<td>874.35</td>
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<td>80.73</td>
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<td>211.57</td>
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<td>96.73</td>
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<td>38.21</td>
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<tr>
<td>85</td>
<td>94.18</td>
<td>98.18</td>
<td>4.00</td>
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<td>98.91</td>
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<td>0.12</td>
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<td>3483.82</td>
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<tr>
<td>96</td>
<td>99.64</td>
<td>100.00</td>
<td>0.36</td>
<td>0.13</td>
<td>3657.64</td>
<td>3613.79</td>
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</table>
Table 3  Key values to describe the relationship between the packet dropper and Pcapreplay

<table>
<thead>
<tr>
<th>Name</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\bar{x}$</td>
<td>50</td>
</tr>
<tr>
<td>$\bar{y}$</td>
<td>39.52</td>
</tr>
<tr>
<td>SSE</td>
<td>1516.56</td>
</tr>
<tr>
<td>SS$_{tot}$</td>
<td>35635.06</td>
</tr>
<tr>
<td>SS$_{reg}$</td>
<td>29328.22</td>
</tr>
<tr>
<td>SS$_{res}$</td>
<td>1516.56</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.96</td>
</tr>
<tr>
<td>ln ($L$)</td>
<td>-14452.8</td>
</tr>
<tr>
<td>AIC</td>
<td>28911.54</td>
</tr>
<tr>
<td>AIC$_c$</td>
<td>28913.14</td>
</tr>
<tr>
<td>BIC</td>
<td>28914.38</td>
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<tr>
<td>resVar</td>
<td>94.78512</td>
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<tr>
<td>$\chi^2_v$</td>
<td>19</td>
</tr>
<tr>
<td>$\chi^2_v$</td>
<td>1.1875</td>
</tr>
</tbody>
</table>

Fig. 9  PLR vs. ALR for CDX gator010 abridged with the packet dropper using the capped-by-packets algorithm and abridged by pcapreplay

We will now look more closely at the Pcapreplay data to determine if there exists a relationship $y = f(x)$, where $y$ is ALR and $x$ is PLR. Observing Fig. 8, we see that the relationship between PLR and ALR is nonlinear. The growth in ALR is slow at the start, and at the end of the PLR domain is an S-shaped pattern. This is the behavior of a sigmoid function illustrated in Formula 11 and Fig. 10. We will use the general logistic function in Formula 12 as the model for our nonlinear regression,
where $A$ is the lower asymptote, $K$ is the upper asymptote, $B$ is the growth rate, $v$ affects near which asymptote maximum growth occurs, $Q$ depends on the value of $y$ when $x = 0$, and $M$ is the time of maximum growth. We were able to use the solver in Microsoft Excel to discover values for $A$, $K$, $B$, $v$, $Q$, and $M$. These values are shown in Table 4 along with the values for several other variables, including the $R^2$ and $\chi^2_v$.

$$y = \frac{1}{(1 + e^{-x})}. \quad (11)$$

![Fig. 10 Sigmoid nonlinear regression model](image)

$$y = A + \frac{K - A}{(1 + e^{-B(x-M)})^{\frac{1}{v}}}. \quad (12)$$
Table 4  Key values of the regression analysis of the impact of SLPL

<table>
<thead>
<tr>
<th>Name</th>
<th>Value</th>
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</thead>
<tbody>
<tr>
<td>A</td>
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</tr>
<tr>
<td>K</td>
<td>100</td>
</tr>
<tr>
<td>B</td>
<td>200.948</td>
</tr>
<tr>
<td>v</td>
<td>2.88963</td>
</tr>
<tr>
<td>Q</td>
<td>0.36356</td>
</tr>
<tr>
<td>M</td>
<td>68.4576</td>
</tr>
<tr>
<td>SSE</td>
<td>2765.56</td>
</tr>
<tr>
<td>(\bar{y})</td>
<td>35.78</td>
</tr>
<tr>
<td>(\bar{x})</td>
<td>48.56429</td>
</tr>
<tr>
<td>SSR</td>
<td>385175.22</td>
</tr>
<tr>
<td>SS_{xy}</td>
<td>386765.96</td>
</tr>
<tr>
<td>SS_{xx}</td>
<td>146326.0840484140</td>
</tr>
<tr>
<td>(R^2)</td>
<td>0.9958896459</td>
</tr>
<tr>
<td>(\ln(L))</td>
<td>-1829.221623</td>
</tr>
<tr>
<td>AIC</td>
<td>3670.443247</td>
</tr>
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<td>AIC_c</td>
<td>3670.803762</td>
</tr>
<tr>
<td>BIC</td>
<td>3691.32708</td>
</tr>
<tr>
<td>resVar</td>
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<tr>
<td>(\chi^2)</td>
<td>240</td>
</tr>
<tr>
<td>(\chi^2_v)</td>
<td>1.025641026</td>
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</table>

5. Conclusions

Through this research we were able to answer each of our research questions in the affirmative. We determined that SLPL is sufficiently regular to allow an algorithm to be developed to model it. We discovered that the capped-by-packets algorithm of the packet dropper, developed in a previous work,\(^2\) models SLPL in this dataset with \(R^2\) and \(\chi^2_v\) values very close to 1. We were able to determine that the impact of SLPL on NID performance is sufficiently regular to allow a formula to be developed that will accurately predict the effect, and we defined a formula that predicts the effect on this dataset with \(R^2\) and \(\chi^2_v\) values very close to 1. We claim that the existence of the packet dropper algorithm that models SLPL accurately for this dataset and the formula that predicts the impact of SLPL on NID performance for this dataset
demonstrate the affirmative answers to our research questions. We make no claim that this algorithm or formula is the correct algorithm or formula to model SLPL or the impact of SLPL in general.

The ultimate goal is to discover a general function $y = f(x)$, where $y$ is ALR and $x$ is PLR. This function will allow us to accurately predict the impact of packet loss on NID. To achieve this goal, a study of the combined effect of packet loss across all 3 layers should be conducted upon the foundation that has been laid by studying each layer individually. The packet dropper algorithm needs to be refined and validated based upon the findings of the combined study. Replaying a dataset at several multiples of its original speed is a time-consuming process even when it may be completely automated. The CDX dataset that we used was originally 105 h long. Replaying the dataset in an exponential progression (i.e., $2^n$) would require 210 h. Often this technique does not produce enough data points, and the process would take even longer. Some of the datasets studied in our previous research are 7 weeks long and would be completely impractical to study by replaying them at several multiples of the original speed. Having a validated packet dropper, which can process the dataset in minutes rather than days, would greatly benefit the research. With a validated packet dropper, it may be possible to analyze several datasets and generate and validate a general function.
6. References


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Appendix. Pcapreplay Linux Online Manual Page
NAME
    pcapreplay − Replays a libpcap file with a given acceleration.

SYNOPSIS
    pcapreplay [options] [pcapfile] ...
    -L --logfile set the file where diagnostic info is written.
    -b --bitbucket set the bit bucket file.
    -h --help print usage information.
    -r --readfile set the readfile.
    -v --version print the version information.
    -w --writefile set the writefile.
    -x --accelerate set acceleration factor.

DESCRIPTION
    Pcapreplay concatenates the files in the pcap format given on the command line and writes them at the
    speed in which they were captured with a user provided acceleration factor. Packets that cannot be written
    in time may optionally be placed in a bit bucket file.

EXAMPLE(S)
    The following command will replay the capture.pcap file at 5 times the original speed to standard output
    over a pipe to snort. Packets that cannot be written in time will be written to the bucket.pcap file.
    $ pcapreplay −x 5 −b bucket.pcap −w - capture.pcap | snort

SEE ALSO
    libpcap(3), tcpdump(8)

AUTHOR(S)
    Sidney C. Smith, Computational Information Sciences Directorate, US Army Research Laboratory
ACRONYMS:

ALR  alert loss rate
CDX  Cyber Defense Exercise
CPU  Central Processing Unit
DRPL detection–relevant packet loss
NID  network intrusion detection
PLR  packet loss rate
SLPL sensor–level packet loss

MATHEMATICAL SYMBOLS:

\( R^2 \) the coefficient of determination

\( \text{SSE} \) sum of the squares of error \( \text{SSE} = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2 \)

\( \text{SS}_{\text{tot}} \) total sum of squares \( \text{SS}_{\text{yy}} = \sum_{i=1}^{n} (y_i - \bar{y})^2 \)

\( \text{SS}_{\text{reg}} \) sum of squares regression \( \text{SS}_{\text{reg}} = \sum_{i=1}^{n} (\hat{y}_i - \bar{y}_i)^2 \)

\( \text{SS}_{\text{res}} \) residual sum of squares \( \text{SS}_{\text{res}} = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2 \)

\( \ln (L) \) maximum log-likelihood \( \ln (L) = 0.5(-N(\ln 2\pi + 1 - \ln N + \ln \sum_{i=1}^{n} x_i^2)) \)

\( \text{AIC} \) Akaike Information Criterion \( \text{AIC} = 2p - 2\ln (L) \)

\( \text{AIC}_c \) bias-corrected AIC \( \text{AIC}_c = \text{AIC} + \frac{2p(p+1)}{n-p-1} \)

\( \text{BIC} \) Bayesian Information Criterion \( \text{BIC} = p\ln (n) - 2\ln (L) \)

\( \text{resVar} \) residual variance \( \text{resVar} = \frac{\text{RSS}}{n-p} \)

\( \chi^2 \) chi-square \( \chi^2 = \sum_{i=1}^{n} \frac{(y_i - f(x_i))^2}{\sigma_i^2} \)

\( \chi_v^2 \) reduced chi-squared \( \chi_v^2 = \frac{\chi^2}{v} \)

\( \sigma_i^2 \) the variance \( \sigma_i^2 = \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{n-1} \)
MATHEMATICAL OPERATORS:

\( \bar{y} \) the bar over the variable indicated the mean value for that variable

\( \hat{y} \) the hat over the variable indicates the value predicted by the regression function