



# **Nozzle Design Influence on the Supersonic Particle Deposition Process**

by

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# Purpose

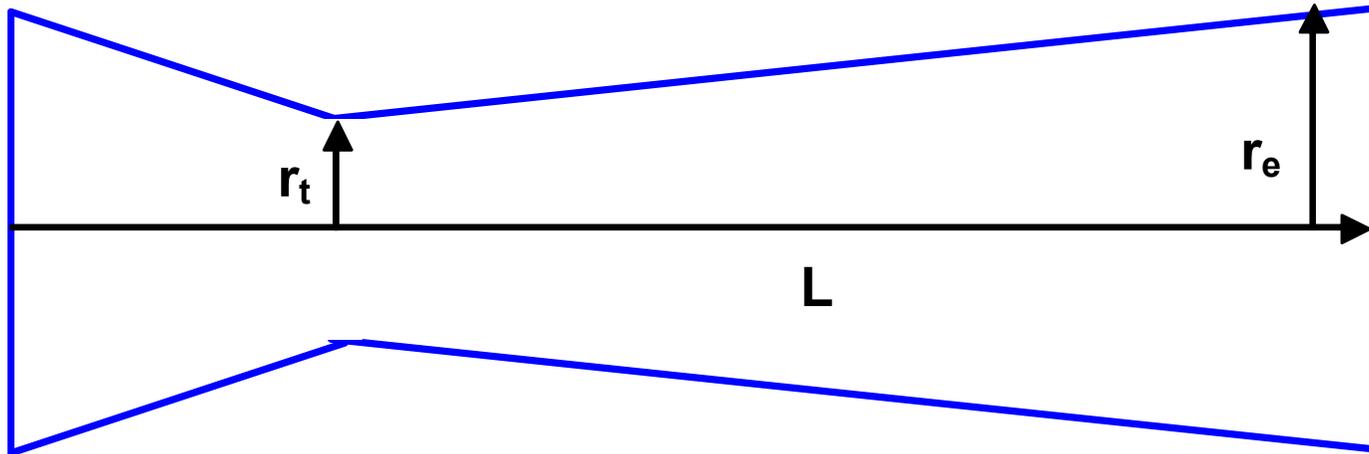
**To improve cold spray deposition through the investigation of:**

- **Nozzle geometry**
- **Accelerating gas characteristics**
- **Particle characteristics**

# Outline

- 1. Calculate the gas flow and temperature in the nozzle**
- 2. Calculate particle velocity and temperature through the nozzle**
- 3. Calculate penetration depth and particle/substrate mixing**
- 4. Calculate the deposition efficiency**
- 5. Compare with experiment**

# Apply Gasdynamic Analysis to Simple Nozzle Geometry



- The gas obeys the perfect gas law
- There is no friction impeding the gas flow
- The gas flow is adiabatic
- No shocks or discontinuities
- Flow is one-dimensional
- Particles do not influence gas conditions

# Particle Motion/Deposition

- Using the gas flow already calculated, employ solid rocket nozzle particle drag and heat transfer relationships\* to calculate particle conditions.
- Particles are assumed to be spherical.
- Particle initial temperature = 293 degree K.
- Use empirical relationships between particle velocity and particle/substrate material characteristics to calculate deposition effects.

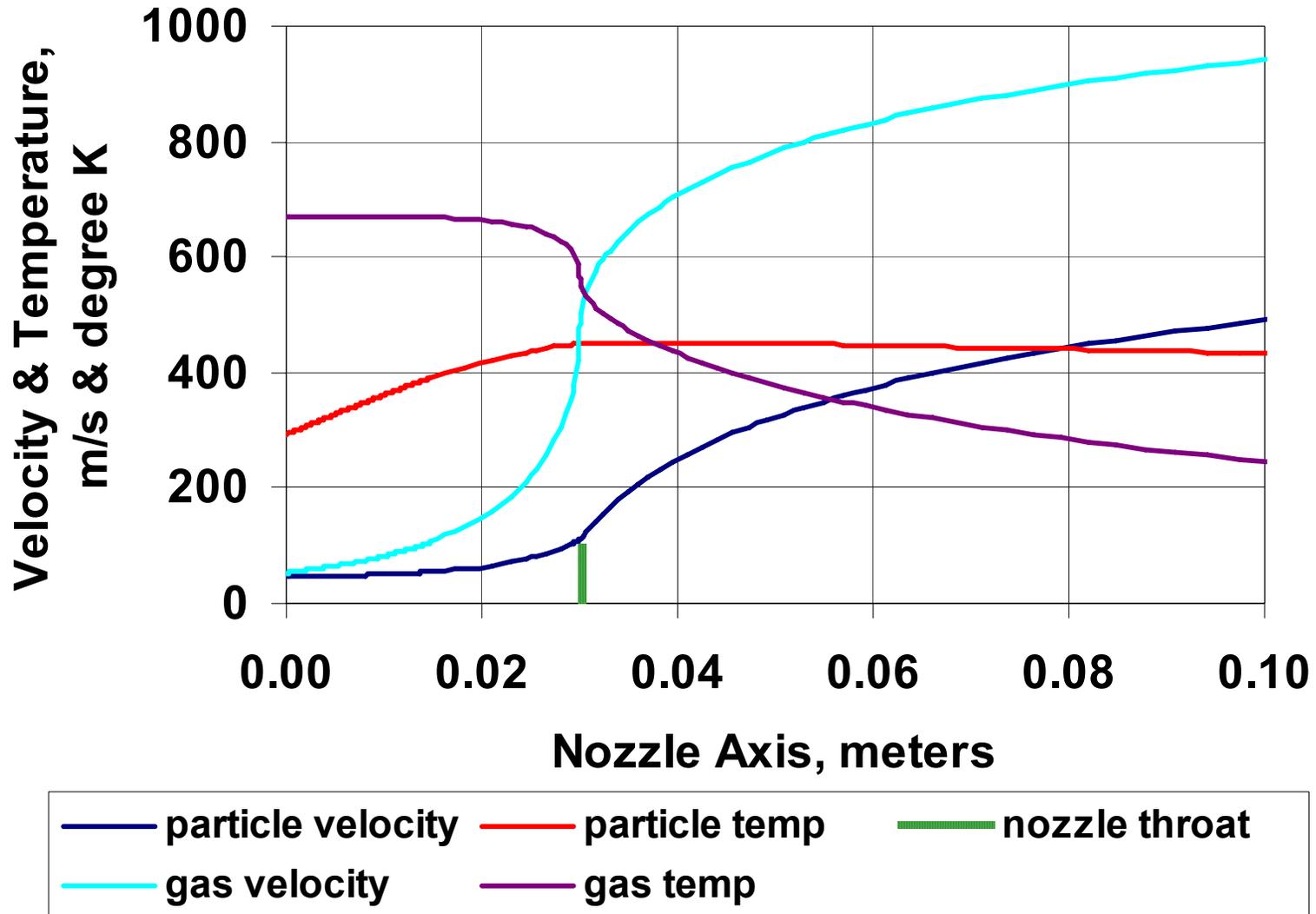
\*D. Carlson and R. Hoglund: "Particle Drag and Heat Transfer in Rocket Nozzles," *AIAA Journal*, 1964, 2(11), pp. 1980 -1984.

# Conditions of Calculations

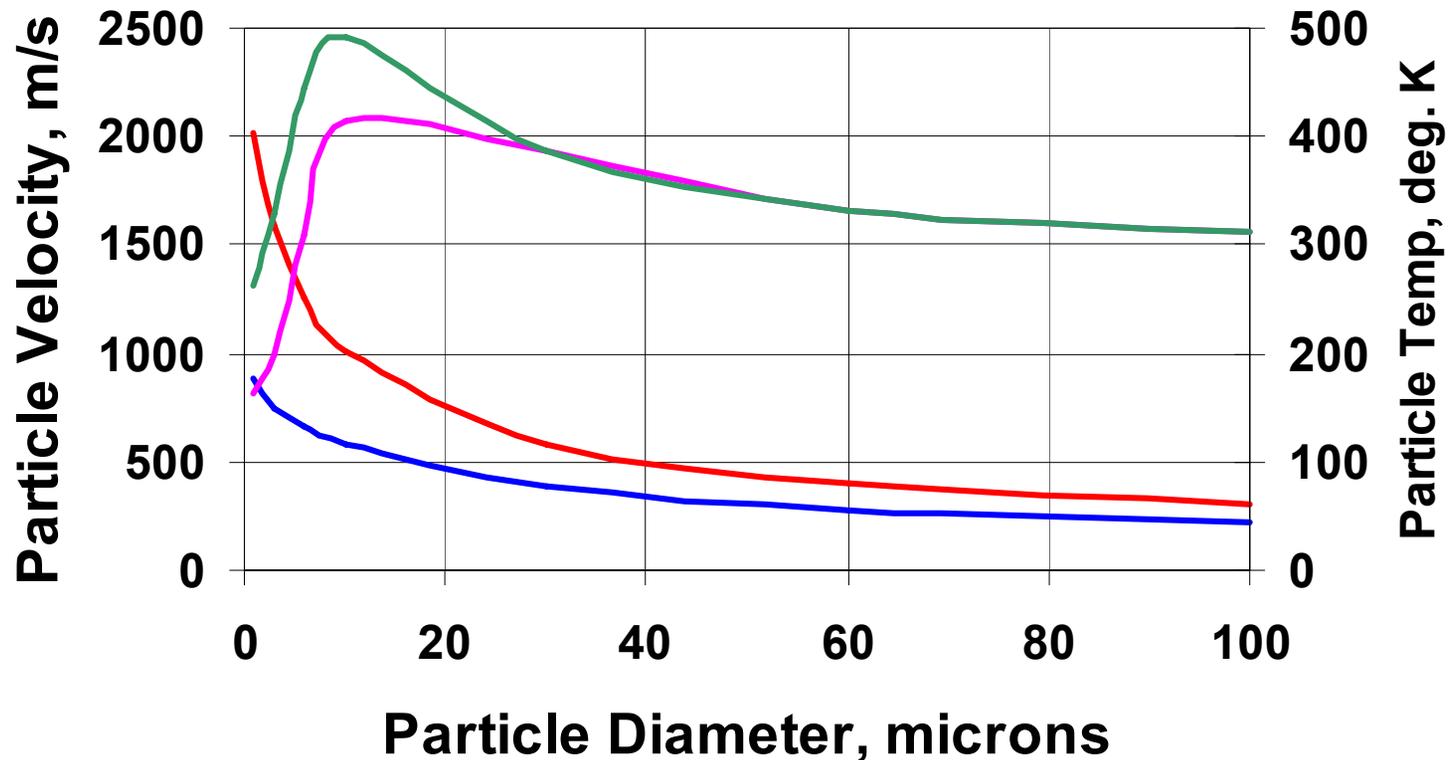
Unless otherwise stated, all calculations are carried out for the following conditions:

- Area ratio = 4, Length = 0.1m
- Nitrogen accelerating gas
- 2.76 MPa, 673 degree K stagnation conditions
- Copper particles
- Mass mean diameter 20 microns
- Log-normal distribution, SD = 1.5

# Typical Calculation

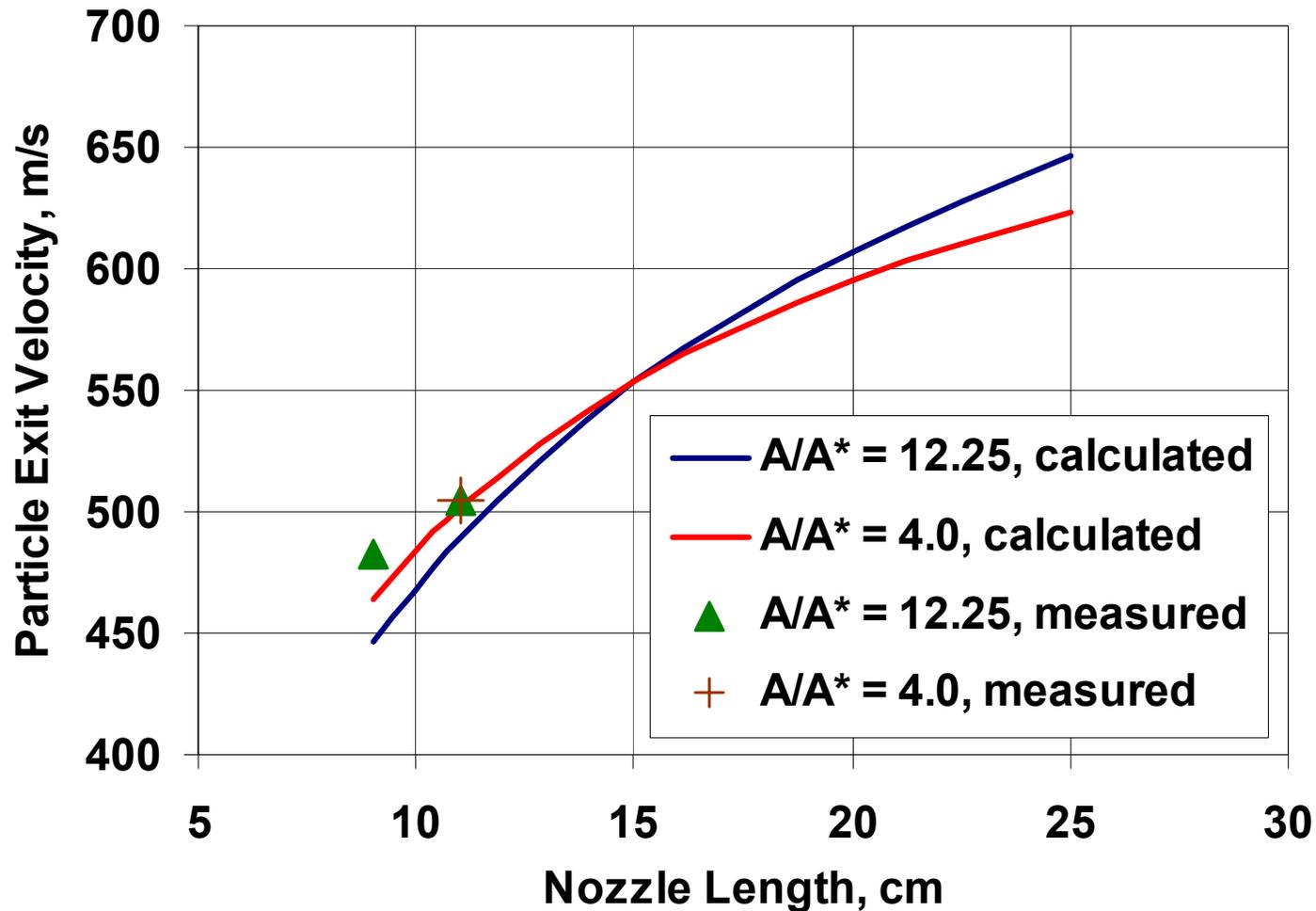


# Particle Exit Conditions as a Function of Diameter and Accelerating Gas



— Velocity, He — Velocity, N2 — Temperature, He — Temperature, N2

# Effect of Nozzle Length on Particle Velocity



# Deposition Calculations

## Particle/Substrate

Empirical micrometeorite penetration into spacecraft\*

$$\text{Volume} = \frac{(4 \times 10^{-5})E}{B}$$

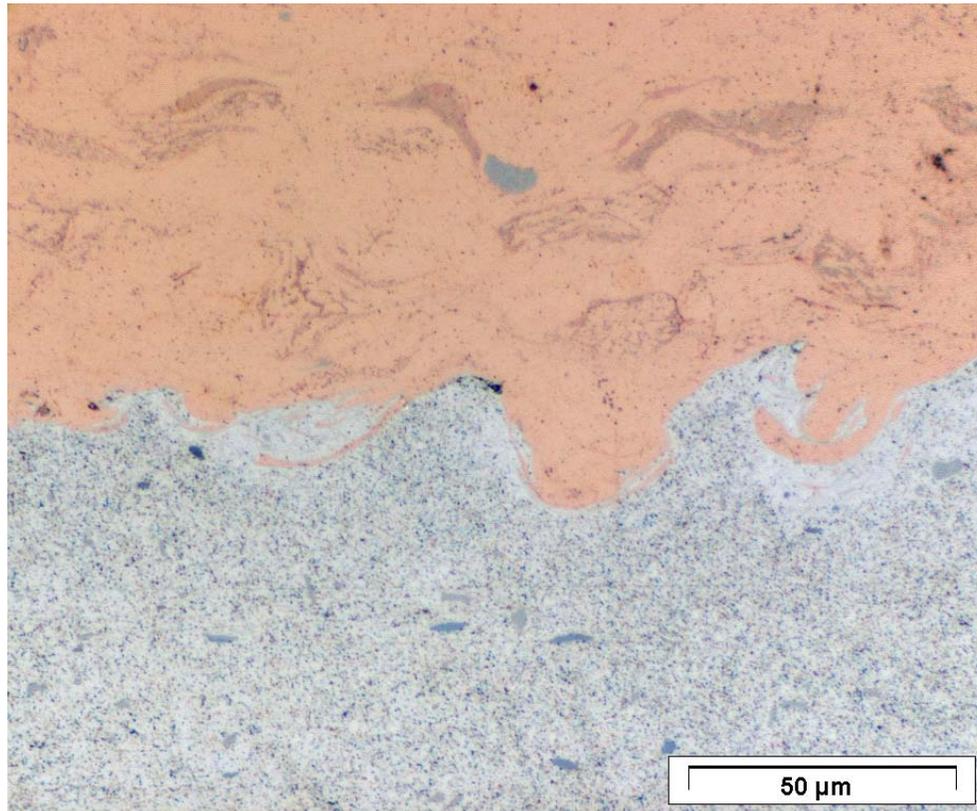
Substituting  $1/2mV^2$  for energy, with volume =  $2r\pi r^2$

$$V = \left[ (7.5 \times 10^4) \left( \frac{B}{\rho} \right) \right]^{0.5}$$

\*R.J. Eichelberger and J.W. Gehring: "Effects of Meteoroid Impacts on Space Vehicles," *ARS J.*, 1963, 32(10), p. 1583.

# Copper Deposited on Aluminum

Particle/substrate equation predicts a velocity of 500 m/s needed for full penetration. Photograph below shows this condition.



# Deposition Calculations

## Particle/Particle

The empirical relationship for the critical velocity is given by Assadi\* as:

$$\text{Critical Velocity} = 667 - 14\rho + 0.08T_m + 0.1\sigma_\mu - 0.4T_e$$

$\rho$  = particle density

$T_m$  = particle melting point

$\sigma_\mu$  = particle UTS

$T_e$  = particle exit temperature

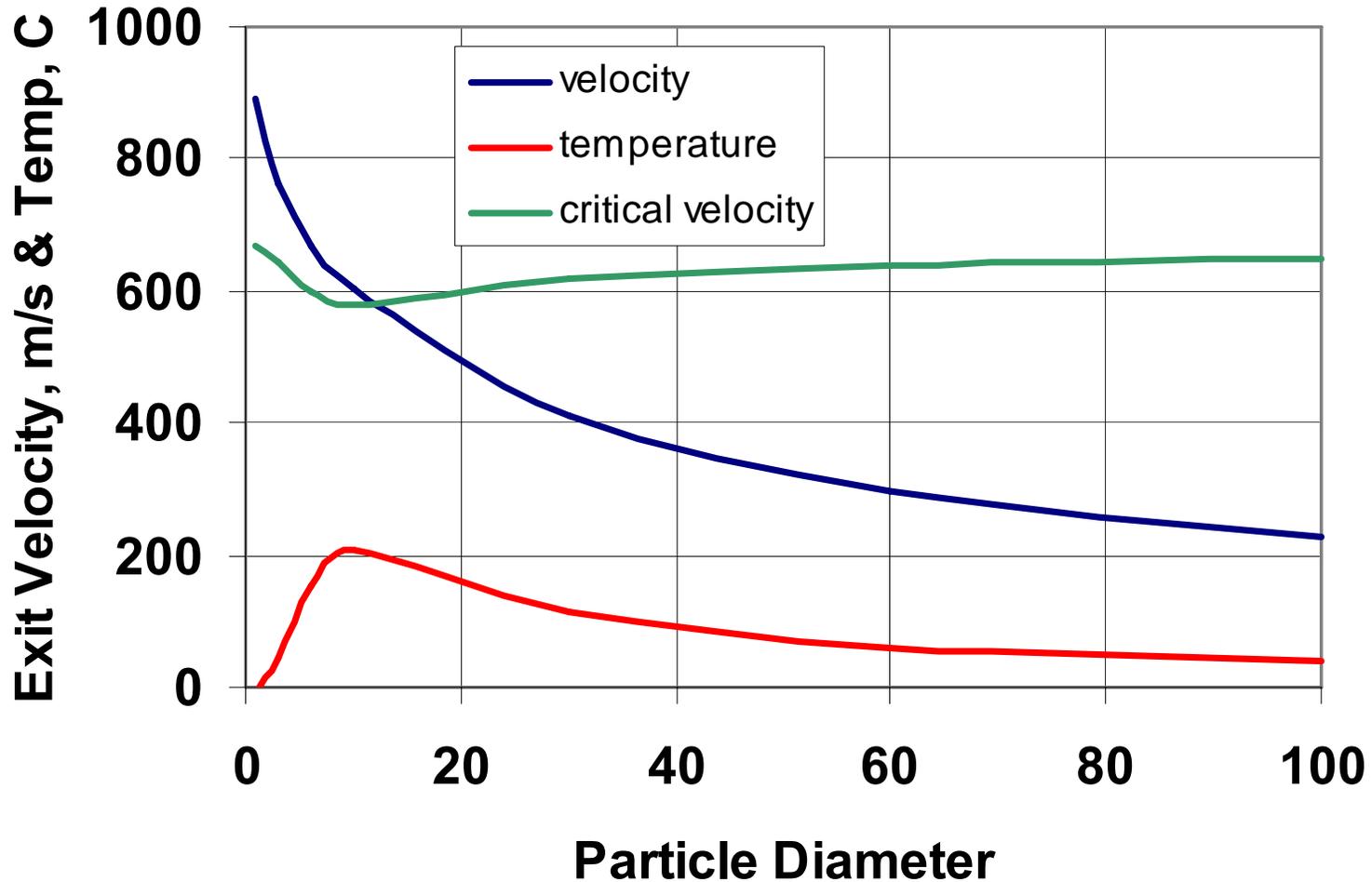
All particles smaller than that exiting with the critical velocity will deposit

\*H. Assadi, et al: "Bonding Mechanism in Cold Gas Spraying,"  
*Acta Materialia*, 2003, 51, pp. 4379 – 4394.

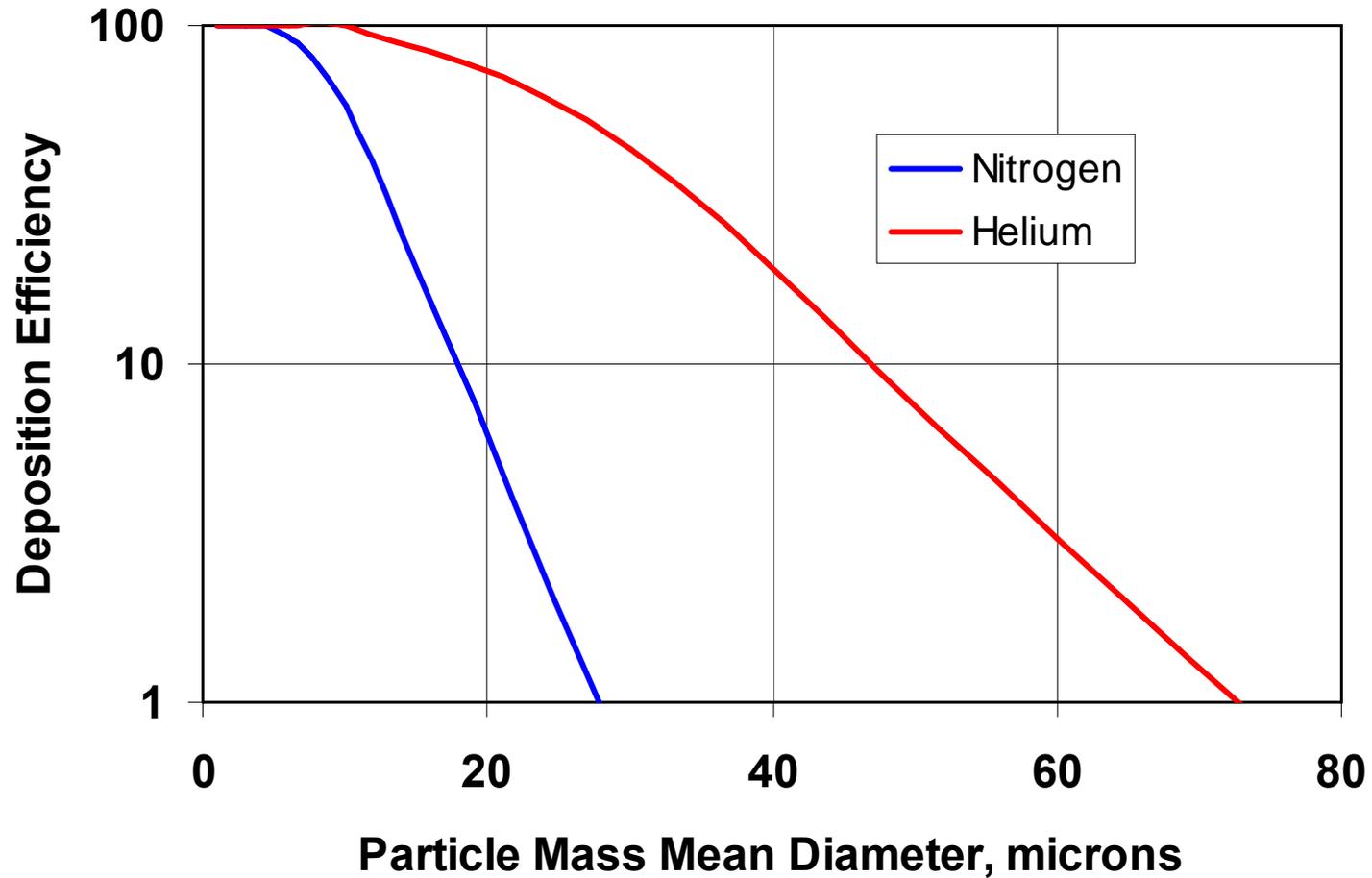
# Deposition Efficiency Calculation

1. Calculate table of particle exit velocities and temperatures vs. particle diameter.
2. Calculate critical velocities based on the particle exit temperatures.
3. Find the critical particle size that has an exit velocity equal to the critical velocity.
4. Integrate the log normal particle size distribution from the critical diameter to 1/infinity.

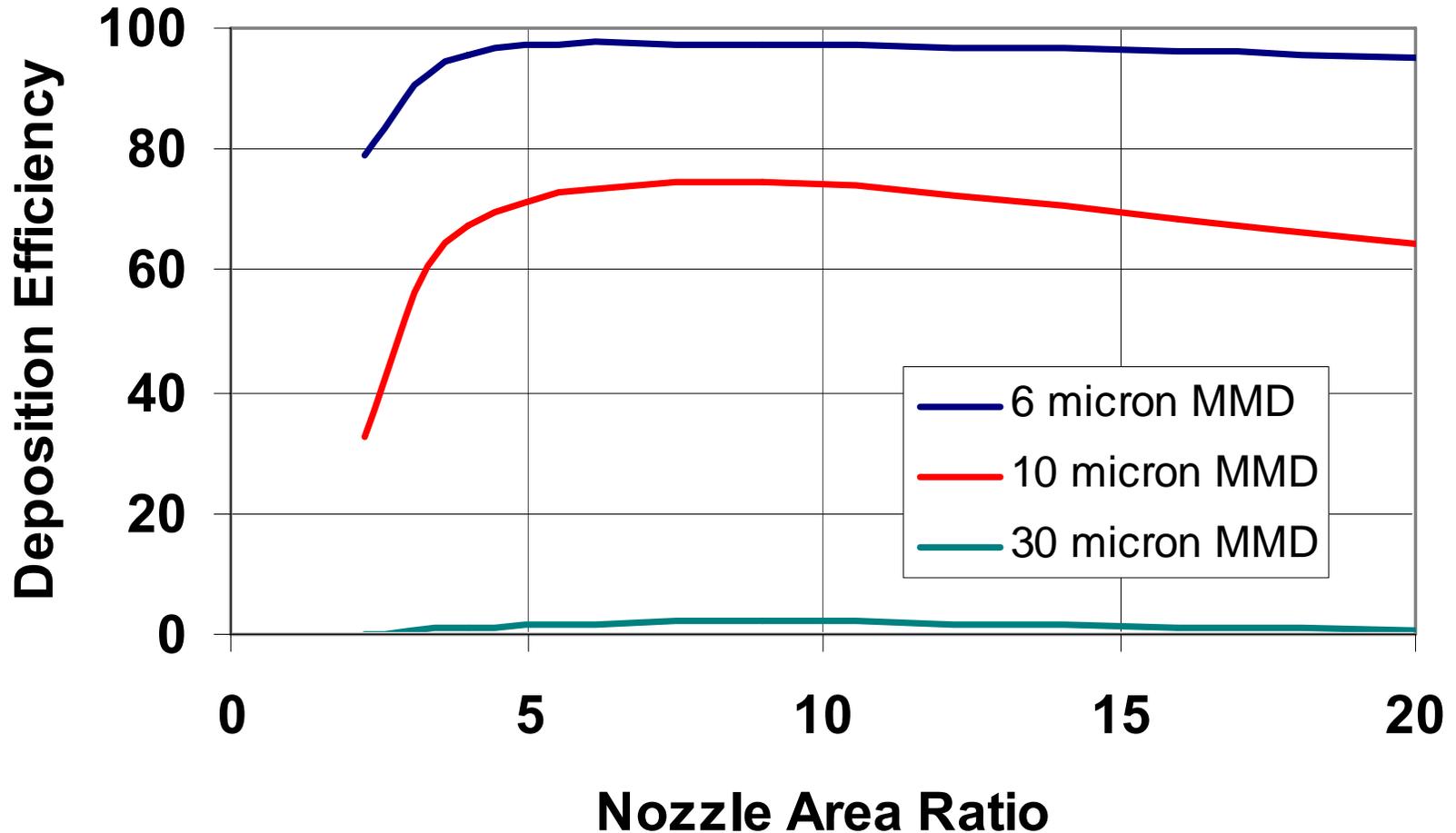
# Critical Particle Diameter



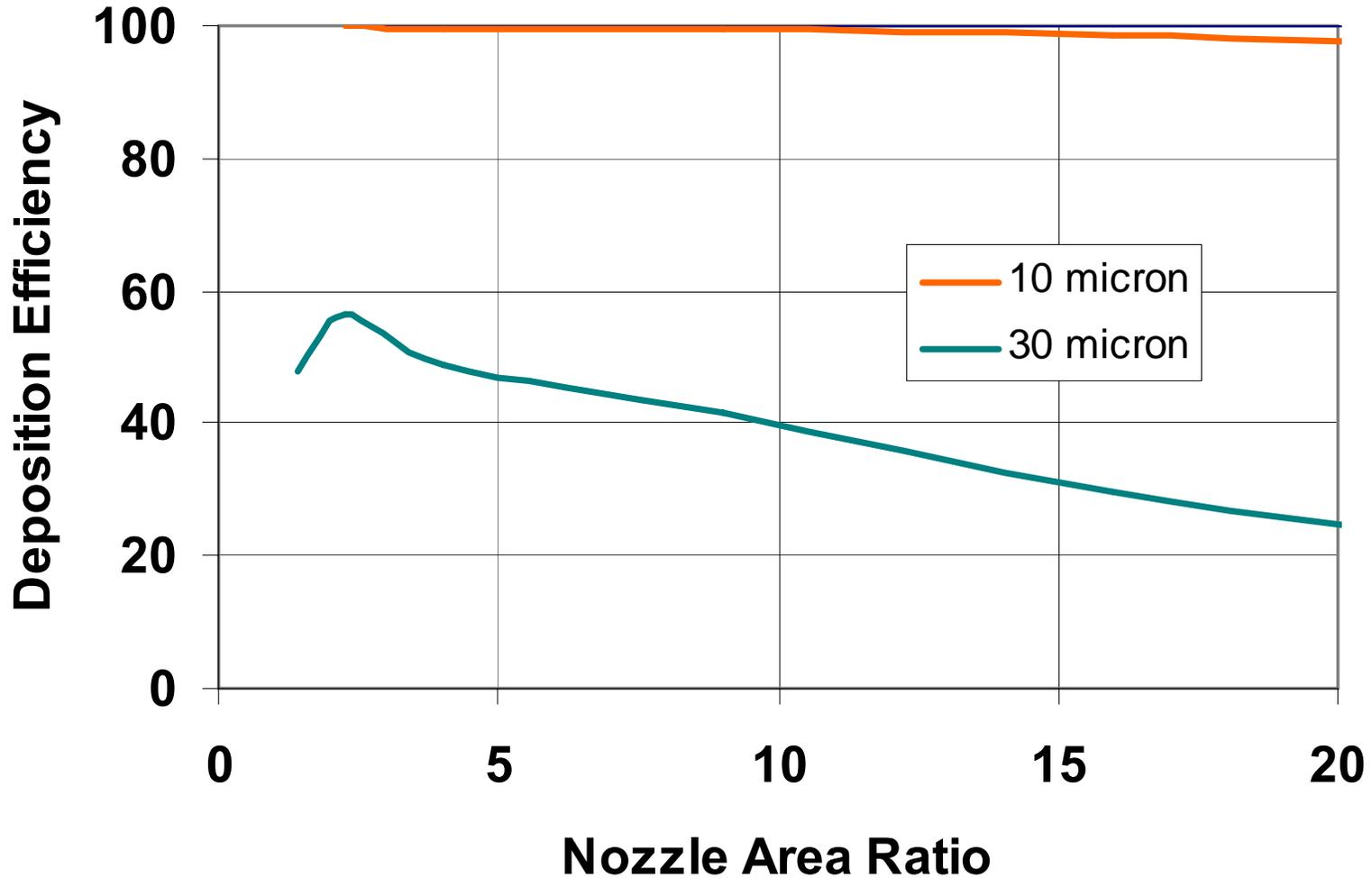
# Effect of Particle Diameter on Deposition Efficiency



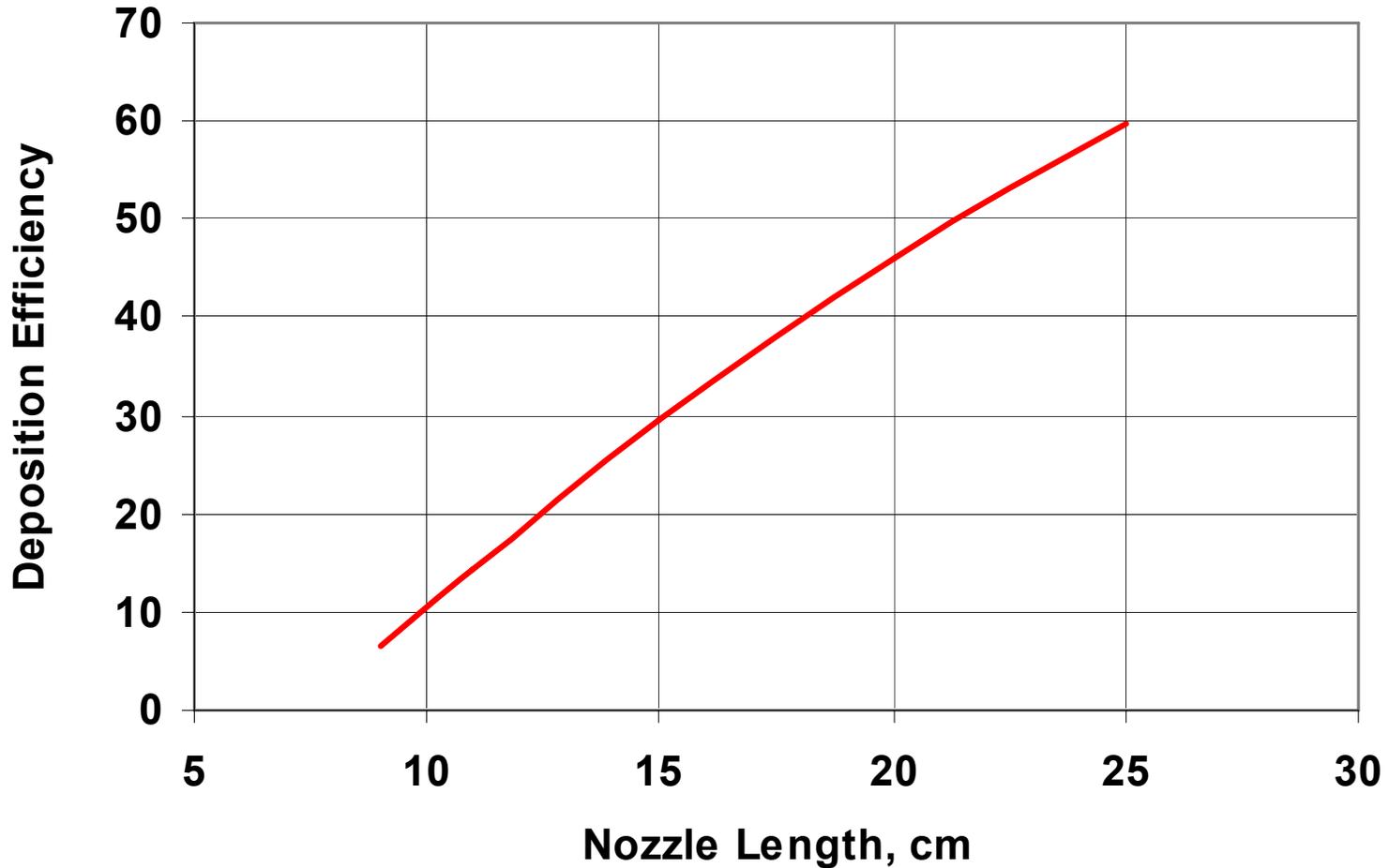
# Effect of Nozzle Area Ratio on Deposition Efficiency



# Effect of Nozzle Area Ratio on Deposition Efficiency - Helium



# Effect of Nozzle Length on Deposition Efficiency



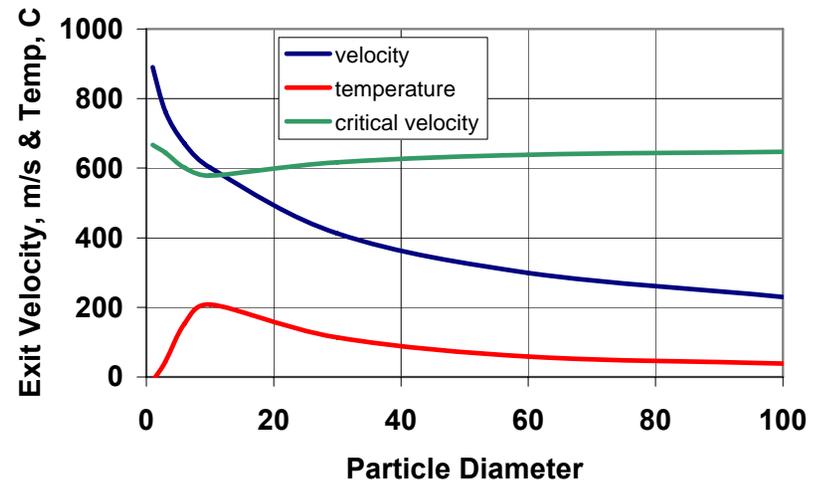
# Conclusions

- Particle exit conditions are principally determined by nozzle length and particle diameter.
- Particle/surface interaction can be characterized by particle velocity and surface hardness.
- Particle velocity and deposition efficiency are relatively insensitive to nozzle area ratio.
- Large improvements to deposition efficiency are possible through the use of smaller particles and longer nozzles.

# Parameters for Calculation

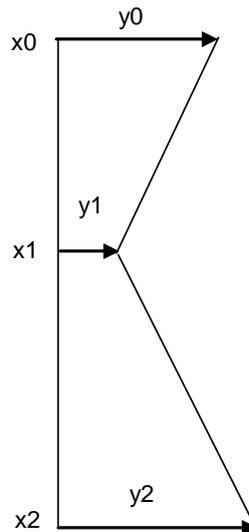
	microns	Vp, m/s	Tp, C	Vc, m/s	Tp critical	critical dia
0.1 M0						
0.001 delM, M<1	1	890	-11	667		
0.05 delM, M>1	3	762	44	645	0	0
673 T0 degK	6	670	153	601	0	0
400 P0 psia	10	602	208	579	0	0
2758000 P0 pascal	30	412	113	617	199	12
28 MW	60	299	58	639	0	0
8314 R	100	230	39	647	0	0
1.4 gamma						
0.9 Vp0/Vg0						
0.001 throat radius m						

Particle Exit Conditions



**10 MMD**  
**67.35 Deposition Efficiency**

same N2-He  
.03N2-.15He



- Fn(M0) y0
- 0.001 y1
- 0.002 y2
- 0 x0
- 0.03 x1
- 0.1 x2
- 4.00 Ae/A\*
- 1.00E-05 reference diameter m
- 9 material density g/cc
- 7.85E-11 particle area m^2
- 4.71E-12 particle mass kg
- 2.00E-05 viscosity kg/m-sec
- 293 Tp0 K
- 390 particle Cp J/kg-K
- 0.03 gas cond. Kg-m/s^3-K
- 1084 melting Point, C
- 345 particle UTS, Mpa
- 12.00 critical diameter
- 1.5 std dev
- 1 ERF sign
- 0.3180 ERF argument

# Effect of Feeder Gas Mixing

